

HVDC Transmission Systems

UNIT-1

Introduction

Electric power transmission was originally developed with direct current. The availability of transformers and the development and improvement of induction motors at the beginning of the 20th century, led to the use of AC transmission.

DC Transmission now became practical when long distances were to be covered or where cables were required. Thyristors were applied to DC transmission and solid state valves became a reality.

With the fast development of converters (rectifiers and inverters) at higher voltages and larger currents, DC transmission has become a major factor in the planning of the power transmission. In the beginning all HVDC schemes used mercury arc valves, invariably single phase in construction, in contrast to the low voltage polyphase units used for industrial application. About 1960 control electrodes were added to silicon diodes, giving silicon-controlled-rectifiers (SCRs or Thyristors).

Today, the highest functional DC voltage for DC transmission is +/- 600kV. D.C transmission is now an integral part of the delivery of electricity in many countries throughout the world.

Comparison of AC and DC Transmission

The merits of two modes of transmission (AC & DC) should be compared based on the following factors.

- 1) Economics of transmission
- 2) Technical Performance
- 3) Reliability

Economics of Power Transmission:

In DC transmission, inductance and capacitance of the line has no effect on the power transfer capability of the line and the line drop. Also, there is no leakage or charging current of the line under steady conditions.

A DC line requires only 2 conductors whereas AC line requires 3 conductors in 3-phase AC systems. The cost of the terminal equipment is more in DC lines than in AC line. Break-even

distance is one at which the cost of the two systems is the same. It is understood from the below figure that a DC line is economical for long distances which are greater than the break-even distance.

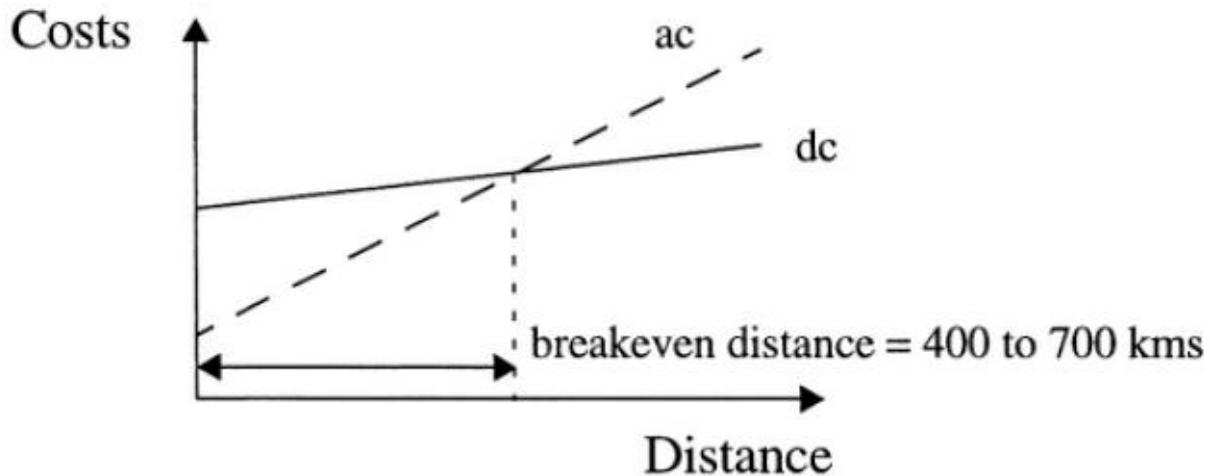


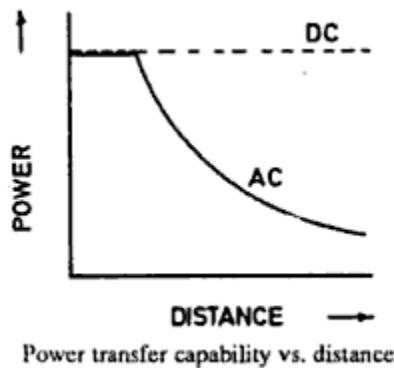
Figure: Relative costs of AC and DC transmission lines vs distance

Technical Performance:

Due to its fast controllability, a DC transmission has full control over transmitted power, an ability to enhance transient and dynamic stability in associated AC networks and can limit fault currents in the DC lines. Furthermore, DC transmission overcomes some of the following problems associated with AC transmission.

Stability Limits:

The power transfer in an AC line is dependent on the angle difference between the voltage phasors at the two line ends. For a given power transfer level, this angle increases with distance. The maximum power transfer is limited by the considerations of steady state and transient stability. The power carrying capability of an AC line is inversely proportional to transmission distance whereas the power carrying ability of DC lines is unaffected by the distance of transmission.



Voltage Control:

Voltage control in ac lines is complicated by line charging and voltage drops. The voltage profile in an AC line is relatively flat only for a fixed level of power transfer corresponding to its Surge Impedance Loading (SIL). The voltage profile varies with the line loading. For constant voltage at the line ends, the midpoint voltage is reduced for line loadings higher than SIL and increased for loadings less than SIL.

The maintenance of constant voltage at the two ends requires reactive power control as the line loading is increased. The reactive power requirements increase with line length. Although DC converter stations require reactive power related to the power transmitted, the DC line itself does not require any reactive power. The steady-state charging currents in AC cables pose serious problems and make the break-even distance for cable transmission around 50kms.

Line Compensation:

Line compensation is necessary for long distance AC transmission to overcome the problems of line charging and stability limitations. The increase in power transfer and voltage control is possible through the use of shunt inductors, series capacitors, Static Var Compensators (SVCs) and, lately, the new generation Static Compensators (STATCOMs). In the case of DC lines, such compensation is not needed.

Problems of AC Interconnection:

The interconnection of two power systems through ac ties requires the automatic generation controllers of both systems to be coordinated using tie line power and frequency signals. Even with coordinated control of interconnected systems, the operation of AC ties can be problematic due to:

1. The presence of large power oscillations which can lead to frequent tripping,
2. Increase in fault level, and
3. Transmission of disturbances from one system to the other.

The fast controllability of power flow in DC lines eliminates all of the above problems. Furthermore, the asynchronous interconnection of two power systems can only be achieved with the use of DC links.

Ground Impedance:

In AC transmission, the existence of ground (zero sequence) current cannot be permitted in steady-state due to the high magnitude of ground impedance which will not only affect efficient power transfer, but also result in telephonic interference. The ground impedance is negligible for DC currents and a DC link can operate using one conductor with ground return (monopolar operation).

The ground return is objectionable only when buried metallic structures (such as pipes) are present and are subject to corrosion with DC current flow. While operating in the monopolar mode, the AC network feeding the DC converter station operates with balanced voltages and currents. Hence, single pole operation of dc transmission systems is possible for extended period, while in AC transmission, single phase operation (or any unbalanced operation) is not feasible for more than a second.

Disadvantages of DC Transmission:

The scope of application of DC transmission is limited by

1. High cost of conversion equipment.
2. Inability to use transformers to alter voltage levels.
3. Generation of harmonics.
4. Requirement of reactive power and
5. Complexity of controls.

Over the years, there have been significant advances in DC technology, which have tried to overcome the disadvantages listed above except for (2). These are

1. Increase in the ratings of a thyristor cell that makes up a valve.
2. Modular construction of thyristor valves.
3. Twelve-pulse (and higher) operation of converters.
4. Use of forced commutation.
5. Application of digital electronics and fiber optics in the control of converters.

Reliability:

The reliability of DC transmission systems is good and comparable to that of AC systems. The reliability of DC links has also been very good.

There are two measures of overall system reliability-energy availability and transient reliability.

Energy availability:

Energy availability = $100 (1 - \frac{\text{equivalent outage time}}{\text{Actual time}}) \%$

Actual time

Where equivalent outage time is the product of the actual outage time and the fraction of system capacity lost due to outage.

Transient reliability:

This is a factor specifying the performance of HVDC systems during recordable faults on the associated AC systems.

Transient reliability = $100 \times \frac{\text{No. of times HVDC systems performed as designed}}{\text{No. of recordable AC faults}}$

No. of recordable AC faults

Recordable AC system faults are those faults which cause one or more AC bus phase voltages to drop below 90% of the voltage prior to the fault.

Both energy availability and transient reliability of existing DC systems with thyristor valves is 95% or more.

Application of DC Transmission

Due to their costs and special nature, most applications of DC transmission generally fall into one of the following three categories.

Underground or underwater cables:

In the case of long cable connections over the breakeven distance of about 40-50 km, DC cable transmission system has a marked advantage over AC cable connections. Examples of this type of applications were the Gotland (1954) and Sardinia (1967) schemes. The recent development of Voltage Source Converters (VSC) and the use of rugged polymer DC cables, with the so-called "HVDC Light" option, are being increasingly considered. An example of this type of application is the 180 MW Direct link connection (2000) in Australia.

Long distance bulk power transmission:

Bulk power transmission over long distances is an application ideally suited for DC transmission and is more economical than ac transmission whenever the breakeven distance is

exceeded. Examples of this type of application abound from the earlier Pacific Intertie to the recent links in China and India.

The breakeven distance is being effectively decreased with the reduced costs of new compact converter stations possible due to the recent advances in power electronics.

Stabilization of power flows in integrated power system:

In large interconnected systems, power flow in AC ties (particularly under disturbance conditions) can be uncontrolled and lead to overloads and stability problems thus endangering system security. Strategically placed DC lines can overcome this problem due to the fast controllability of DC power and provide much needed damping and timely overload capability. The planning of DC transmission in such applications requires detailed study to evaluate the benefits. Example is the Chandrapur-Padghe link in India.

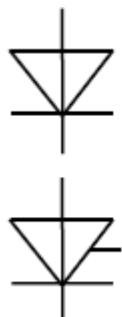
Presently the number of DC lines in a power grid is very small compared to the number of AC lines. This indicates that DC transmission is justified only for specific applications. Although advances in technology and introduction of Multi-Terminal DC (MTDC) systems are expected to increase the scope of application of DC transmission, it is not anticipated that the AC grid will be replaced by a DC power grid in the future. There are two major reasons for this:

First, the control and protection of MTDC systems is complex and the inability of voltage transformation in dc networks imposes economic penalties.

Second, the advances in power electronics technology have resulted in the improvement of the performance of AC transmissions using FACTS devices, for instance through introduction of static VAR systems, static phase shifters, etc.

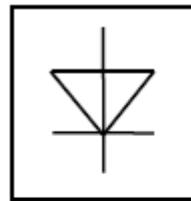
Types of Valves

Based on the controllability and configuration valves are classified into four types as under.

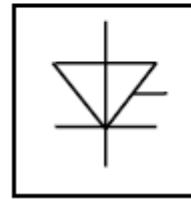


Non-controllable valve or arm

Controllable valve or arm



Non-controllable bridge or valve group

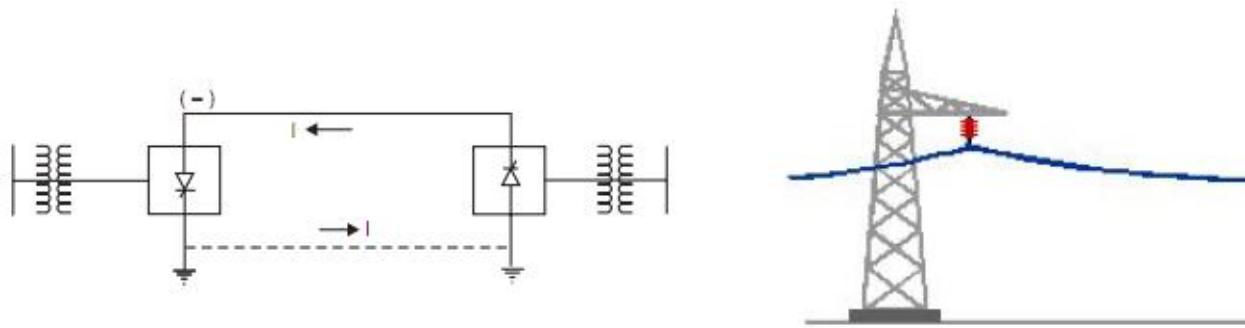


Controllable bridge or valve group

Types of HVDC Links

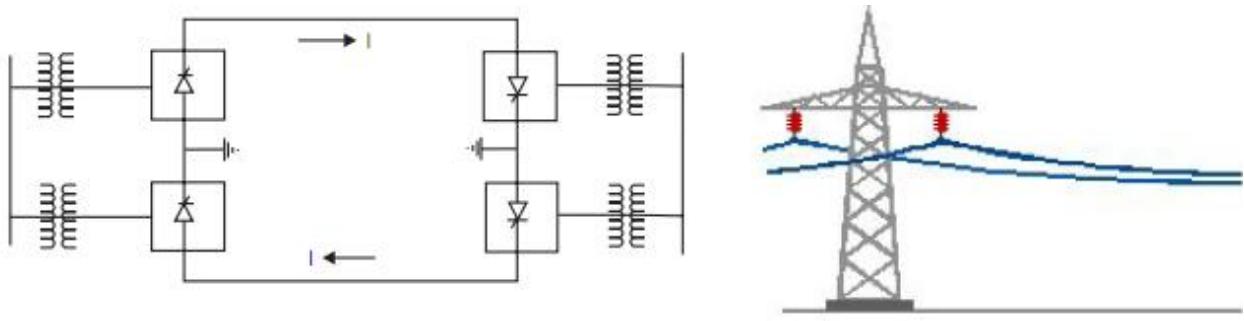
Three types of HVDC Links are considered in HVDC applications which are

Monopolar Link:



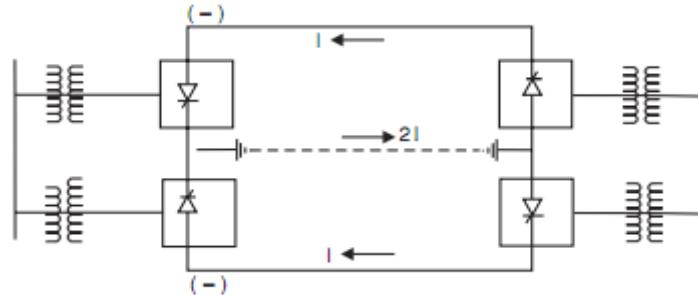
A monopolar link as shown in the above figure has one conductor and uses either ground and/or sea return. A metallic return can also be used where concerns for harmonic interference and/or corrosion exist. In applications with DC cables (i.e., HVDC Light), a cable return is used. Since the corona effects in a DC line are substantially less with negative polarity of the conductor as compared to the positive polarity, a monopolar link is normally operated with negative polarity.

Bipolar Link:



A bipolar link as shown in the above figure has two conductors, one positive and the other negative. Each terminal has two sets of converters of equal rating, in series on the DC side. The junction between the two sets of converters is grounded at one or both ends by the use of a short electrode line. Since both poles operate with equal currents under normal operation, there is zero ground current flowing under these conditions. Monopolar operation can also be used in the first stages of the development of a bipolar link. Alternatively, under faulty converter conditions, one DC line may be temporarily used as a metallic return with the use of suitable switching.

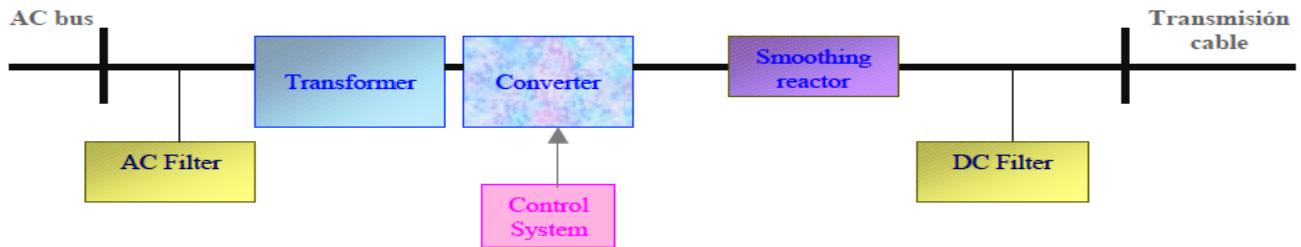
Homopolar Link:



In this type of link as shown in the above figure two conductors having the same polarity (usually negative) can be operated with ground or metallic return.

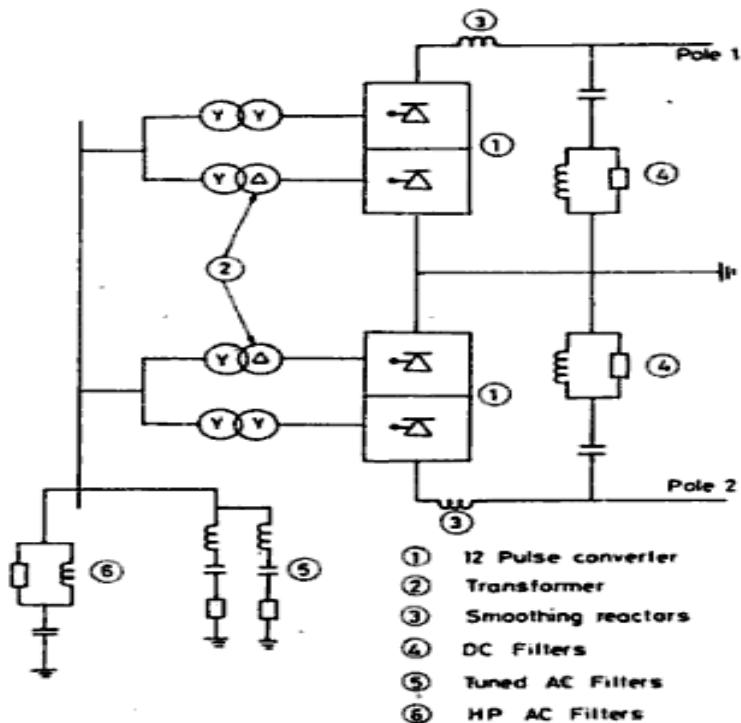
Due to the undesirability of operating a DC link with ground return, bipolar links are mostly used. A homopolar link has the advantage of reduced insulation costs, but the disadvantages of earth return outweigh the advantages.

HVDC Converter Station

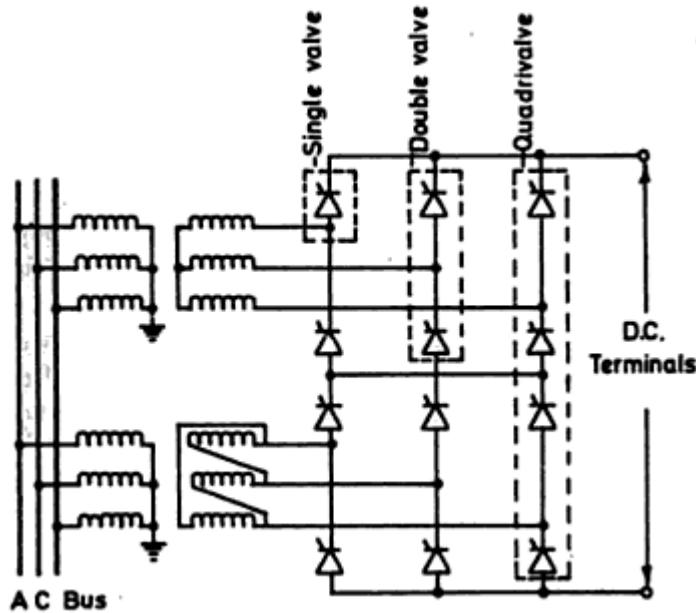


The major components of a HVDC transmission system are converter stations where conversions from AC to DC (Rectifier station) and from DC to AC (Inverter station) are performed. A point to point transmission requires two converter stations. The role of rectifier and inverter stations can be reversed (resulting in power reversals) by suitable converter control.

A typical converter station with two 12 pulse converter units per pole is shown in figure below. The block diagram of converter station is given above.



Converter Unit:



This usually consists of two three phase converter bridges connected in series to form a 12 pulse converter unit as shown in above figure. The total number of valves in such a unit is twelve. The valves can be packaged as single valve, double valve or quadrivalve arrangements. Each valve is used to switch in segment of an AC voltage waveform. The converter is fed by converter transformers connected in star/star and star/delta arrangements.

The valves are cooled by air, oil, water or freon. Liquid cooling using deionized water is more efficient and results in the reduction of station losses. The design of valves is based on the modular concept where each module contains a limited number of series connected thyristor levels.

Valve firing signals are generated in the converter control at ground potential and are transmitted to each thyristor in the valve through a fiber optic light guide system.

The valves are protected using snubber circuits, protective firing and gapless surge arrestors.

Converter Transformer:

The converter transformer has three different configurations-

- (i) three phase, two winding,
- (ii) single phase, three winding and
- (iii) single phase, two winding

The valve side windings are connected in parallel with neutral grounded. The leakage reactance of the transformer is chosen to limit the short circuit currents through any valves.

The converter transformers are designed to withstand DC voltage stresses and increased eddy current losses due to harmonic currents. One problem that can arise is due to the DC magnetization of the core due to unsymmetrical firing of valves.

Filters:

There are three types of filters used which are

1. AC Filters:

These are passive circuits used to provide low impedance, shunt paths for AC harmonic currents. Both tuned and damped filter arrangements are used.

2. DC Filters:

These are similar to AC filters and are used for the filtering of DC harmonics.

3. High Frequency (RF/PLC) Filters:

These are connected between the converter transformer and the station AC bus to suppress any high frequency currents. Sometimes such filters are provided on high-voltage DC bus connected between the DC filter and DC line and also on the neutral side.

Reactive power source:

Converter stations require reactive power supply that is dependent on the active power loading. But part of the reactive power requirement is provided by AC filters. In addition, shunt capacitors, synchronous condensors and static VAR systems are used depending on the speed of control desired.

Smoothing Reactor:

A sufficiently large series reactor is used on DC side to smooth DC current and also for protection. The reactor is designed as a linear reactor and is connected on the line side, neutral side or at intermediate location.

DC Switchgear:

It is modified AC equipment used to interrupt small DC currents. DC breakers or Metallic Return Transfer Breakers (MRTB) are used, if required for interruption of rated load currents.

In addition to the DC switchgear, AC switchgear and associated equipment for protection and measurement are also part of the converter station.

Modern Trends in DC Transmission

To overcome the losses and faults in AC transmission, HVDC transmission is preferred.

The trends which are being introduced are for the effective development to reduce the cost of the converters and to improve the performance of the transmission system.

Power semiconductors and valves:

The IGBTs or GTOs employed required huge amount of current to turn it ON which was a big problem. GTOs are available at 2500V and 2100A. As the disadvantage of GTOs is the large gate current needed to turn them OFF, so MCT which can be switched OFF by a small current is preferred as valves.

The power rating of thyristors is also increased by better cooling methods. Deionized water cooling has now become a standard and results in reduced losses in cooling.

Converter Control:

The development of micro-computer based converter control equipment has made possible to design systems with completely redundant converter control with automatic transfer between systems in the case of a problem.

The micro-computer based control also has the flexibility to implement adaptive control algorithms or even the use of expert systems for fault diagnosis and protection.

DC Breakers:

Parallel rather than series operation of converters is likely as it allows certain flexibility in the planned growth of a system. The DC breaker ratings are not likely to exceed the full load ratings as the control intervention is expected to limit the fault current.

Conversion of existing AC lines:

There are some operational problems due to electromagnetic induction from AC circuits where an experimental project of converting a single circuit of a double circuit is under process.

Operation with weak AC systems:

The strength of AC systems connected to the terminals of a DC link is measured in terms of Short Circuit Ratio (SCR) which is defined as

$\text{SCR} = \frac{\text{Short circuit level at the converter bus}}{\text{Rated DC Power}}$

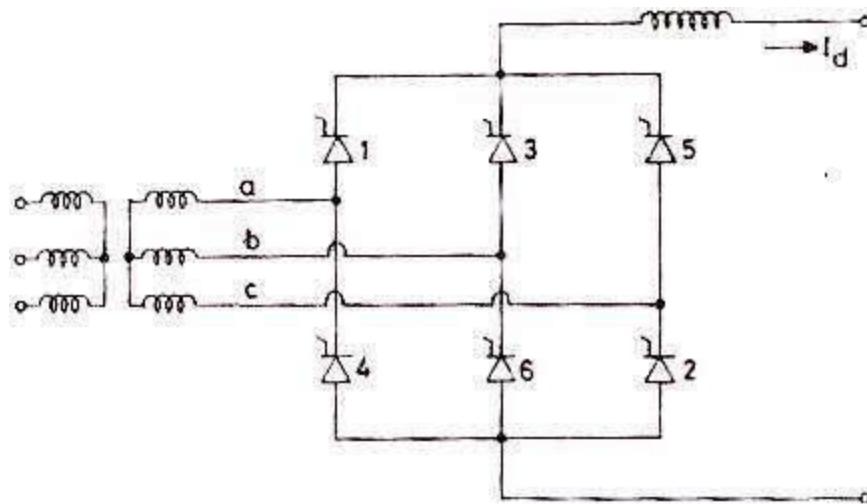
If SCR is less than 3, the AC system is said to be weak. The conventional constant extinction angle control may not be suitable for weak AC systems.

Constant reactive current control or AC voltage control may overcome some of the problems of weak AC systems.

The power modulation techniques used to improve dynamic stability of power systems will have to be modified in the presence of weak AC systems.

Six Pulse Converters

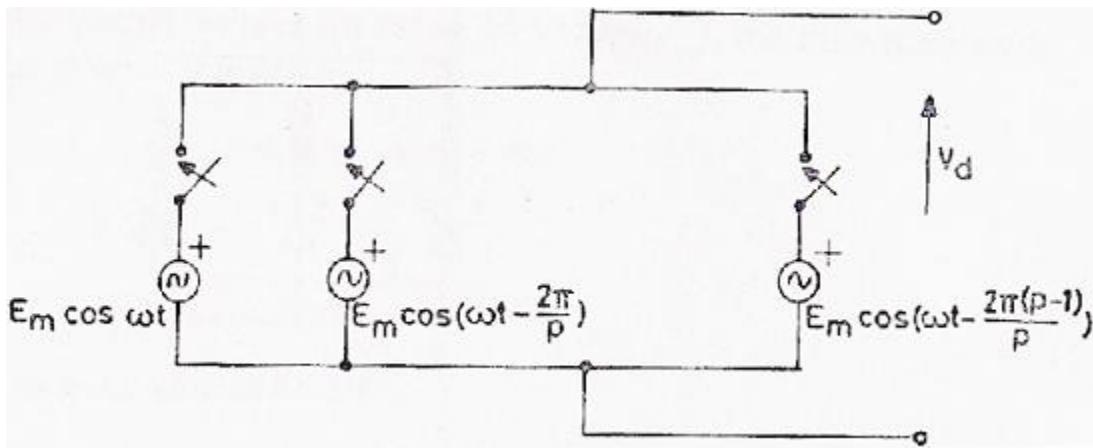
The conversion from AC to DC and vice-versa is done in HVDC converter stations by using three phase bridge converters. The configuration of the bridge (also called Graetz circuit) is a six pulse converter and the 12 pulse converter is composed of two bridges in series supplied from two different (three-phase) transformers with voltages differing in phase by 30° .



Pulse Number

The pulse number of a converter is defined as the number of pulsations (cycles of ripple) of direct voltage per cycle of alternating voltage.

The conversion from AC to DC involves switching sequentially different sinusoidal voltages onto the DC circuit.

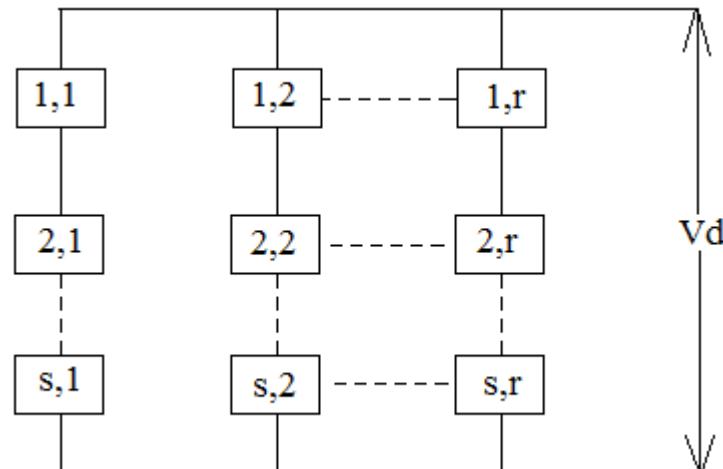


A valve can be treated as a controllable switch which can be turned ON at any instant, provided the voltage across it is positive.

The output voltage V_d of the converter consists of a DC component and a ripple whose frequency is determined by the pulse number

Choice of Converter Configuration

The configuration for a given pulse number is so chosen in such a way that the valve and transformer are used to the maximum.



A converter configuration can be defined by the basic commutation group and the number of such groups connected in series and parallel.

If there are 'q' valves in a basic commutation group and r of those are connected in parallel and s of them in series then,

$$p = q r s$$

Note:

A commutation group is defined as the group of valves in which only one (neglecting overlap) conducts at a time.

Valve Rating:

The valve rating is specified in terms of Peak Inverse Voltage (PIV). The ratio of PIV to average DC voltage is an index of valve utilization.

So, average maximum DC voltage across the converter is given by,

$$\begin{aligned}
 V_{do} &= s \frac{q}{2\pi} \int_{-\pi/q}^{\pi/q} E_m \cos \omega t d(\omega t) \\
 &= s \frac{q}{2\pi} E_m (\sin \omega t) \Big|_{-\pi/q}^{\pi/q} = \frac{sq}{2\pi} E_m \left[\sin \frac{\pi}{q} - \sin \left(-\frac{\pi}{q} \right) \right] = \frac{sq}{2\pi} E_m \cdot 2 \sin \frac{\pi}{q} \\
 V_{do} &= \frac{sq}{\pi} E_m \sin \frac{\pi}{q} \quad \text{----- (1)}
 \end{aligned}$$

If 'q' is even, then maximum inverse voltage occurs when the valve with a phase displacement of 180° is conducting and is given by,

$$\text{PIV} = 2E_m$$

If 'q' is odd, then maximum inverse voltage occurs when the valve with a phase shift of $\pi \pm (\pi/q)$ is conducting and is given by,

$$\text{PIV} = 2E_m \cos(\pi/2q)$$

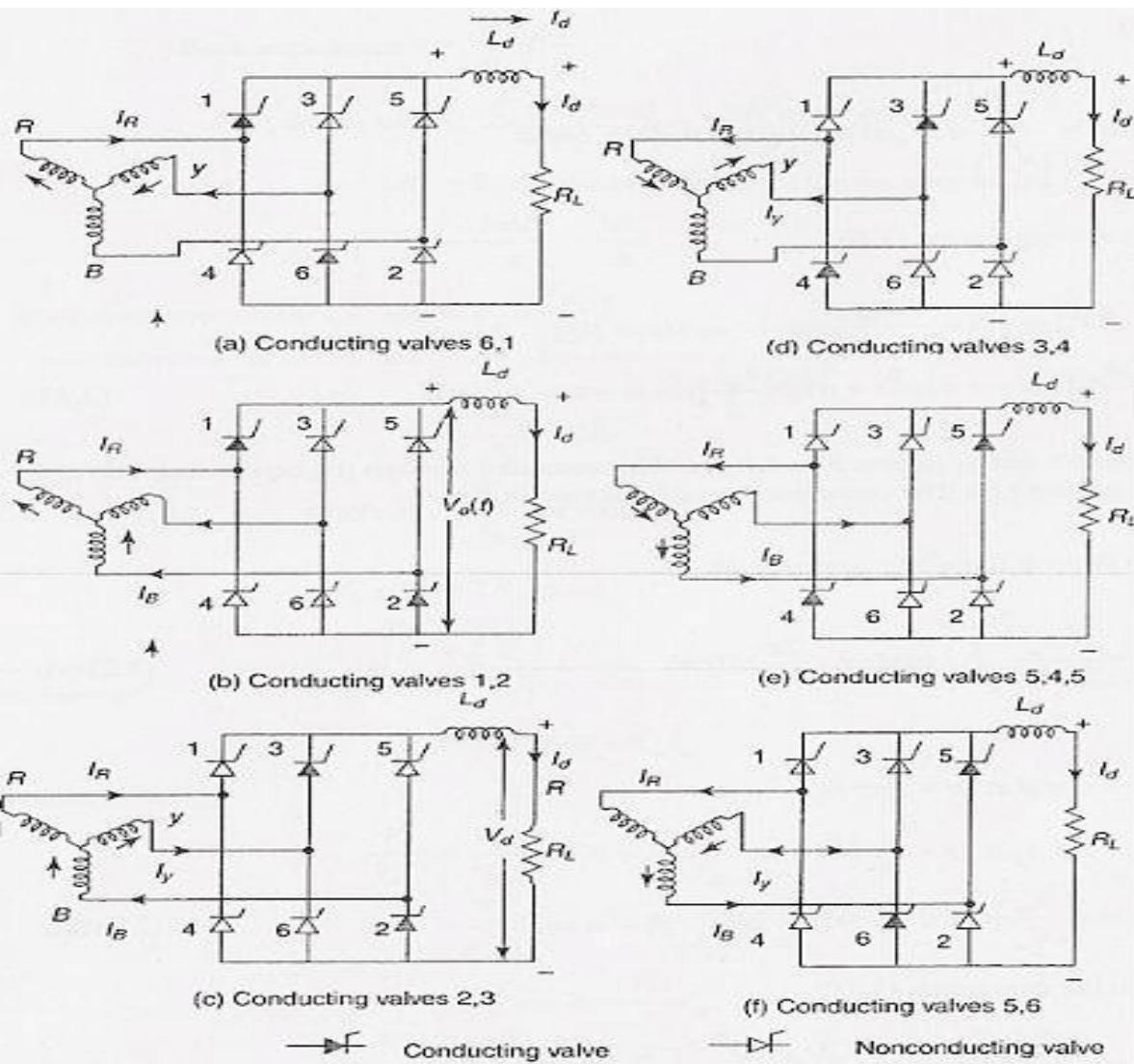
The valve utilization factor is given by

$$\text{For } q \text{ even, } \frac{\text{PIV}}{V_{do}} = \frac{2E_m}{\frac{sq}{\pi} E_m \sin \frac{\pi}{q}} = \frac{2\pi}{s \cdot q \cdot \sin \frac{\pi}{q}}$$

$$\text{For } q \text{ odd, } \frac{\text{PIV}}{V_{do}} = \frac{2E_m \cos \frac{\pi}{2q}}{\frac{sq}{\pi} E_m \sin \frac{\pi}{q}} = \frac{2\pi \cdot \cos \frac{\pi}{2q}}{sq \cdot \sin \frac{\pi}{q}} = \frac{2\pi \cdot \cos \frac{\pi}{2q}}{sq \cdot 2 \cos \frac{\pi}{2q} \sin \frac{\pi}{2q}}$$

$$(\text{Since } \sin 2\theta = 2 \sin \theta \cos \theta \text{ and } 2 \cos \frac{\pi}{2q} \sin \frac{\pi}{2q} = \sin \frac{2\pi}{2q} = \sin \frac{\pi}{q})$$

$$\frac{PIV}{V_{do}} = \frac{\pi}{sq \cdot \sin \frac{\pi}{2q}} \quad (\text{For } q \text{ odd})$$



Transformer Rating:

The current rating of a valve is given by,

$$I_v = \frac{I_d}{r\sqrt{q}} \quad \text{--- (2)}$$

where, \$I_d\$ is the DC current which is assumed to be constant.

The transformer rating on the valve side (in VA) is given by,

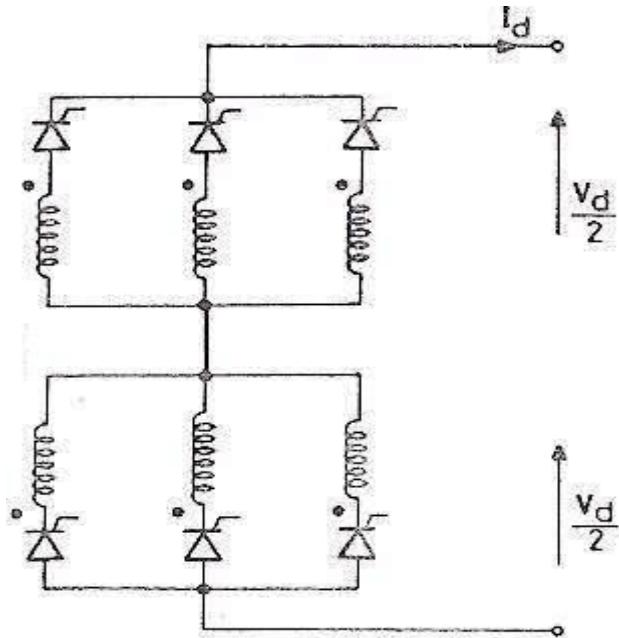
$$S_{tv} = p \frac{E_m}{\sqrt{2}} I_v$$

From equations (1), (2) & $p=qrs$, we have

$$S_{tv} = p \frac{V_{do} \cdot \pi}{\sqrt{2} \cdot sq \cdot \sin \frac{\pi}{q}} \cdot \frac{I_d}{r \sqrt{q}}$$

$$S_{tv} = \frac{\pi}{\sqrt{2}} \cdot \frac{V_{do} I_d}{\sqrt{q} \cdot \sin \frac{\pi}{q}}$$

Transformer utilization factor $\left(\frac{S_{tv}}{V_{do} I_d} \right)$ is a function of q .



As AC supply is three phase so, commutation group of three valves can be easily arranged. So, for $q = 3$,

$$\frac{S_{tv}}{V_{do} I_d} = \frac{\pi}{\sqrt{(2 \times 3)} \sin \frac{\pi}{3}}$$

$$\frac{S_{tv}}{V_{do} I_d} = \frac{\pi}{\sqrt{6} \sin 60^\circ}$$

$$\frac{S_{tv}}{V_{do} I_d} = 1.48$$

Transformer utilization can be improved if two valve groups can share single transformer winding. In this case, the current rating of the winding can be increased by a factor of $\sqrt{2}$ while decreasing the number of windings by a factor of 2.

It is a 6-pulse converter consisting of two winding transformer where the transformer utilization factor is increased when compared to three winding transformer.

The series conduction of converter groups has been preferred because of controlling and protection as well as the requirements for high voltage ratings. So, a 12 pulse converter is obtained by series connection of two bridges.

The 30° phase displacement between two sets of source voltages is achieved by transformer connections Y-Y for one bridge and Y- Δ for the other bridge.

The use of a 12 pulse converter is preferable over the 6 pulse converter because of the reduced filtering requirements.

Analysis of Graetz Circuit without overlap:

At any instant, two valves are conducting in the bridge, one from the upper commutation group and the second from the lower commutation group. The firing of the next valve in a particular group results in the turning OFF of the valve that is already conducting. The valves are numbered in the sequence in which they are fired. Each valve conducts for 120° and the interval between consecutive firing pulse is 60° in steady state.

The following assumptions are made to simplify the analysis

- The DC current is constant.
- The valves are modeled as ideal switches with zero impedance when ON and with infinite impedance when OFF.
- The AC voltages at the converter bus are sinusoidal and remain constant.

One period of the AC supply voltage can be divided into 6 intervals – each corresponding to the conduction of a pair of valves. The DC voltage waveform repeats for each interval.

Assuming the firing of valve 3 is delayed by an angle α , the instantaneous DC voltage V_d during the interval is given by

$$V_d = e_b - e_c = e_{bc} \quad \text{for } \alpha \leq \omega t \leq \alpha + 60^\circ$$

$$\text{Let } e_{ba} = \sqrt{2}E_{LL} \sin \omega t$$

$$\text{then } e_{bc} = \sqrt{2}E_{LL} \sin(\omega t + 60^\circ)$$

$$\text{Average DC Voltage} = V_d = \frac{3}{\pi} \int_{\alpha}^{\alpha+60^\circ} \sqrt{2}E_{LL} \sin(\omega t + 60^\circ) d\omega t$$

$$= \frac{3}{\pi} \sqrt{2}E_{LL} [\cos(\alpha + 60^\circ) - \cos(\alpha + 120^\circ)]$$

$$V_d = \frac{3\sqrt{2}}{\pi} E_{LL} \cos \alpha = 1.35 E_{LL} \cos \alpha$$

$$V_d = V_{do} \cos \alpha \quad \text{----- (1)}$$

The above equation indicates that for different values of α , V_d is variable.

The range of α is 180° and correspondingly V_d can vary from V_{do} to $-V_{do}$. Thus, the same converter can act as a rectifier or inverter depending upon whether the DC voltage is positive or negative.

DC Voltage Waveform:

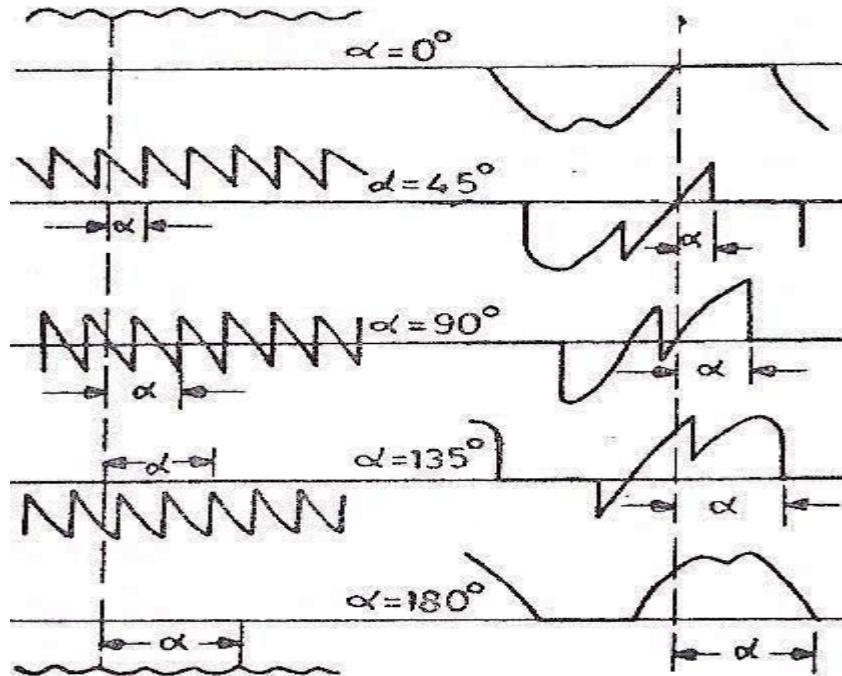
The DC voltage waveform contains a ripple whose fundamental frequency is six times the supply frequency. This can be analyzed in Fourier series and contains harmonics of the order $h = np$

where, p is the pulse number and n is an integer.

The rms value of the h^{th} order harmonic in DC voltage is given by

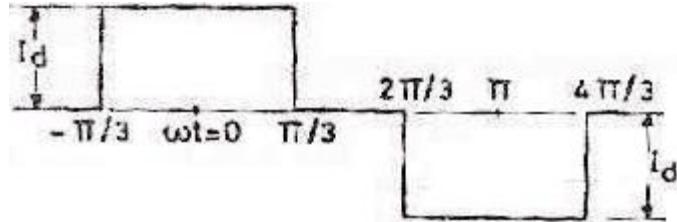
$$V_h = V_{do} \frac{\sqrt{2}}{h^2 - 1} [1 + (h^2 + 1) \sin^2 \alpha]^{1/2}$$

The waveforms of the direct voltage and valve voltage are shown for different values of α .



AC Current Waveform:

It is assumed that direct current has no ripple (or harmonics). The AC currents flowing through the valve (secondary) and primary windings of the converter transformer contain harmonics.



The waveform of the current in a valve winding is shown. The rms value of the fundamental component of current is given by

$$I_1 = \frac{1}{\sqrt{2}} \frac{2}{\pi} \int_{-\pi/3}^{\pi/3} I_d \cos \theta d\theta = \frac{\sqrt{6}}{\pi} I_d \quad \text{--- (2)}$$

where as the rms value of the current is

$$I = \sqrt{\frac{2}{3}} \cdot I_d$$

The harmonics contained in the current waveform are of the order given by

$$h = np \pm 1$$

Where n is an integer, p is the pulse number. For a six pulse converter, the order of AC harmonics is 5, 7, 11, 13 and higher order. These are filtered out by using tuned filters for each one of the first four harmonics and a high pass filter for the remaining.

The rms value of h^{th} harmonic is given by $I_h = \frac{I_1}{h}$

Power Factor:

The AC power supplied to the converter is given by

$$P_{AC} = \sqrt{3} E_{LL} I_1 \cos \phi$$

Where $\cos \phi$ is the power factor.

The DC power must match the AC power ignoring the losses in the converter. Thus,

$$P_{AC} = P_{DC} = V_{do} I_d = \sqrt{3} E_{LL} I_1 \cos \phi$$

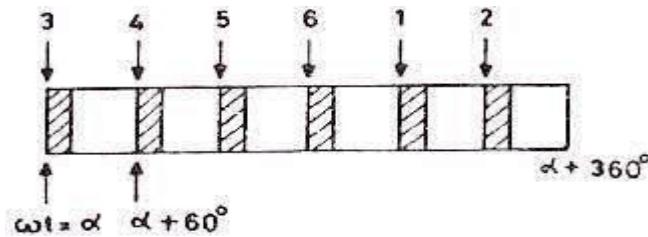
Substituting for V_{do} and I_1 from equations (1) and (2) in the above equation, we get
 $\cos \phi = \cos \alpha$

The reactive power requirements are increased as α is increased from zero (or reduced from 180°).

Analysis of Graetz Circuit with overlap

Due to the leakage inductance of the converter transformers and the impedance in the supply network, the current in a valve cannot change suddenly and this commutation from one valve to the next cannot be instantaneous. This is called overlap and its duration is measured by the overlap (commutation) angle ' μ '.

Each interval of the period of supply can be divided into two subintervals as shown in the below timing diagram. In the first subinterval, three valves are conducting and in the second subinterval, two valves are conducting which is based on the assumption that the overlap angle is less than 60° .



There are three modes of the converter which are

- Mode 1 – Two and three valve conduction ($\mu < 60^\circ$)
- Mode 2 – Three valve conduction ($\mu = 60^\circ$)
- Mode 3 – Three and four valve conduction ($\mu > 60^\circ$)

i) Analysis of Two and Three Valve Conduction Mode:

The equivalent circuit for three valve conduction is shown below.

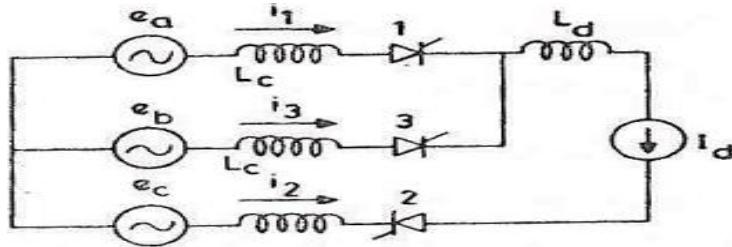
For this circuit,

$$e_b - e_a = L_c \left(\frac{di_3}{dt} - \frac{di_1}{dt} \right)$$

The LHS in the above equation is called the commutating emf whose value is given by

$$e_b - e_a = \sqrt{2} E_{LL} \sin \omega t$$

Which is the voltage across valve 3 just before it starts conducting.



Since, $i_1 = I_d - i_3$

We get,

$$\sqrt{2}E_{LL} \sin \omega t = 2L_c \frac{di_3}{dt}$$

Solving the above equation, we get

$$i_3(t) = I_s (\cos \alpha - \cos \omega t), \alpha \leq \omega t \leq \alpha + \mu$$

Where,

$$I_s = \frac{\sqrt{2}E_{LL}}{2\omega L_c}$$

$$\text{At } \omega t = \alpha + \mu, i_s = I_d. \text{ This gives } I_d = I_s [\cos \alpha - \cos(\alpha + \mu)]$$

The average direct voltage can be obtained as

$$V_d = \frac{3}{\pi} \left[\int_{\alpha}^{\alpha+\mu} \frac{3}{2} e_c d(\omega t) + \int_{\alpha+\mu}^{\alpha+60} (e_b - e_c) d(\omega t) \right]$$

$$= V_{do} \cos \alpha - \frac{3}{2\pi} \sqrt{2}E_{LL} [\cos \alpha - \cos(\alpha + \mu)]$$

$$\text{Since, } \frac{3\sqrt{2}}{\pi} E_{LL} = V_{do}, \text{ we get}$$

$$V_d = \frac{V_{do}}{2} [\cos \alpha + \cos(\alpha + \mu)]$$

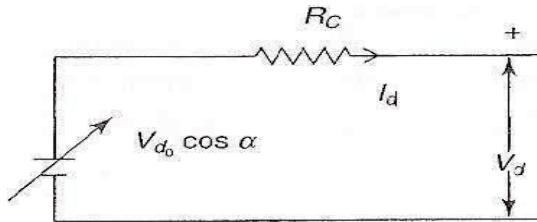
The value of $[\cos \alpha + \cos(\alpha + \mu)]$ can be substituted to get,

$$V_d = V_{do} \left(\cos \alpha - \frac{I_d}{2I_s} \right) = V_{do} \cos \alpha - R_c I_d$$

Where,

$$R_c = \frac{3}{\pi} \omega L_c = \frac{3}{\pi} X_c$$

R_c is called equivalent commutation resistance and the equivalent circuit for a bridge converter is shown below.



Inverter Equations:

For an inverter, advance angle β is given by

$$\beta = \pi - \alpha$$

and use opposite polarity for the DC voltage with voltage rise opposite to the direction of current. Thus,

$$\begin{aligned} V_{di} &= \frac{-V_{doi}}{2} [\cos \alpha + \cos(\alpha + \mu)] \\ &= \frac{-V_{doi}}{2} [\cos(\pi - \beta) + \cos(\pi - \gamma)] \\ V_{di} &= \frac{V_{doi}}{2} [\cos \beta + \cos \gamma] \end{aligned}$$

Where, the extinction angle γ is defined as

$$\gamma = \beta - \mu = \pi - \alpha - \mu$$

Similarly, it can be shown that

$$\begin{aligned} V_{di} &= V_{doi} \cos \beta + R_{ci} I_d \\ &= V_{doi} \cos \gamma - R_{ci} I_d \end{aligned}$$

The subscript "i" refers to the inverter.

ii) Analysis of Three and Four Valve Conduction Mode:

The equivalent circuit for three and four valve conduction is shown below.

For, $\alpha \leq \omega t \leq \alpha + \mu - 60^\circ$

$$i_1 = I_s \sin(\omega t + 60^\circ) + A$$

$$i_6 = I_d - i_2 = I_d - I_s \sin \omega t + C$$

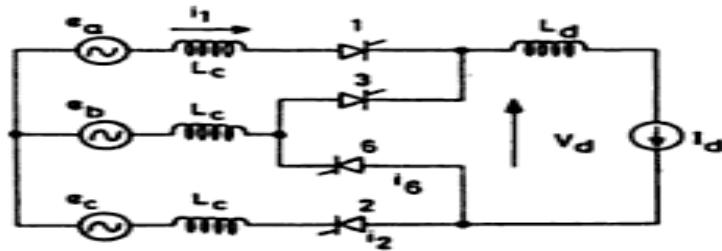
$$\text{Where, } I_s = \frac{E_m}{\omega L_c} = \frac{2}{\sqrt{3}} I_s$$

The constant A can be determined from the initial condition

$$i_1 (\omega t = \alpha) = I_d = I_s \sin(\alpha + 60^\circ) + A$$

The constant C can be determined from the final condition

$$i_6 (\omega t = \alpha + \mu - 60^\circ) = 0 = I_d - I_s \sin(\alpha + \mu - 60^\circ) + C = 0$$



For, $\alpha + \mu - 60^\circ \leq \omega t \leq \alpha + 60^\circ$

$$i_1 = I_s \cos \omega t + B$$

The constant B can be determined from the continuity equation

$$i_1 (\omega t = \alpha + \mu = 60^\circ) = I_s \sin(\alpha + \mu) + A = I_s \cos(\alpha + \mu - 60^\circ) + B$$

Finally,

$$I_d = \frac{I_s}{2} [\cos(\alpha - 30^\circ) - \cos(\alpha + \mu + 30^\circ)]$$

The expression for average direct voltage is given by

$$V_d = \frac{3}{\pi} \int_{\alpha+\mu-60^\circ}^{\alpha+60^\circ} \frac{-3}{2} e_c d(\omega t)$$

Since $e_c = E_m \cos\omega t$

$$V_d = \frac{3}{\pi} \frac{3}{2} E_m [\sin(\alpha + 60^\circ) - \sin(\alpha + \mu - 60^\circ)]$$

$$V_d = \frac{\sqrt{3}}{2} V_{do} [\cos(\alpha - 30^\circ) + \cos(\alpha + \mu + 30^\circ)]$$

Finally

$$V_d = V_{do} [\sqrt{3} \cos(\alpha - 30^\circ) - \frac{3}{2} \frac{I_d}{I_s}] = \sqrt{3} V_{do} \cos(\alpha - 30^\circ) - 3 R_c I_d$$

Converter Bridge Characteristics

A) Rectifier: The rectifier has three modes of operation.

- 1) First mode: Two and three valve conduction mode ($\mu < 60^\circ$)
- 2) Second mode: Three valve conduction mode only for $\alpha < 30^\circ$ ($\mu = 60^\circ$)
- 3) Third mode: Three and four valve conduction mode $\alpha \geq 30^\circ$ ($60^\circ \leq \mu \leq 120^\circ$)

As the DC current continues to increase, the converter operation changes over from mode 1 to 2 and finally to mode 3.

The DC voltage continues to decrease until it reaches zero.

For $\alpha \geq 30^\circ$, mode 2 is bypassed.

For Modes 1 and 3, we have

$$\frac{V_d}{V_{do}} = \cos \alpha - \frac{I_d}{2I_s}$$

$$\frac{V_d}{V_{do}} = \sqrt{3} \cos(\alpha - 30^\circ) - \frac{3I_d}{2I_s}$$

The voltage and current characteristics are linear with different slopes in these cases.

For mode 2, $\mu = 60^\circ$, μ is constant, so the characteristics are elliptical and is given by

$$\left(\frac{V_d^\perp}{\cos \frac{\mu}{2}} \right)^2 + \left(\frac{I_d^\perp}{\sin \frac{\mu}{2}} \right)^2 = 1$$

$$\text{where, } V_d^\perp = \frac{V_d}{V_{do}} \text{ and } I_d^\perp = \frac{I_d}{2I_s}$$

B) Inverter:

The inverter characteristics are similar to the rectifier characteristics. However, the operation as an inverter requires a minimum commutation margin angle during which the voltage across the valve is negative. Hence the operating region of an inverter is different from that for a rectifier.

So, the margin angle (ξ) has different relationship to γ depending on the range of operation which are

First Range: $\beta < 60^\circ$ and $\xi = \gamma$

Second Range: $60^\circ < \beta < 90^\circ$ and $\xi = 60^\circ - \mu = \gamma - (\beta - 60^\circ)$

Third Range: $\beta > 90^\circ$ and $\xi = \gamma - 30^\circ$

In the inverter operation, it is necessary to maintain a certain minimum margin angle ξ_0 which results in 3 sub-modes of the 1st mode which are

Mode 1

1(a) $\beta < 60^\circ$ for values of $\mu < (60^\circ - \xi_0)$

The characteristics are linear defined by

$$V_d^\perp = \cos \gamma_0 - I_d^\perp$$

1(b) $60^\circ < \beta < 90^\circ$ for

$$\mu = 60^\circ - \xi_0 = 60^\circ - \gamma_0 = \text{constant}$$

The characteristics are elliptical.

1(c) $90^\circ < \beta < 90^\circ + \xi_0$ for values of μ in the range

$$60^\circ - \xi_0 \leq \mu \leq 60^\circ$$

The characteristics in this case are line and defined by

$$V_d^l = \cos(\gamma_0 + 30^\circ) - I_d^l$$

Mode 2

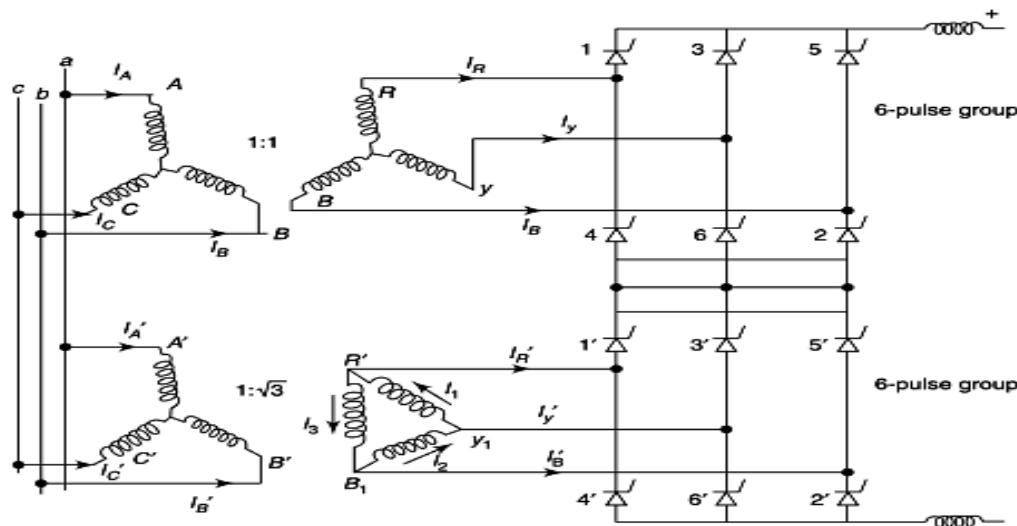
For $\mu > 60^\circ$ corresponding to $\beta > 90^\circ + \gamma_0$

The characteristics again are linear but with a different slope and is defined by

$$V_d^l = \sqrt{3} \cos \gamma_0 - 3I_d^l$$

In the normal operation of the converter I_d^l is in the range of 0.08 to 0.1.

Characteristics of a twelve pulse converter



As long as the AC voltages at the converter bus remain sinusoidal (with effective filtering), the operation of one bridge is unaffected by the operation of the other bridge connected in series. The region of rectifier operation can be divided into five modes as

Mode 1: 4 and 5 valve conduction

$$0 < \mu < 30^\circ$$

Mode 2: 5 and 6 valve conduction

$$30^\circ < \mu < 60^\circ$$

Mode 3: 6 valve conduction

$$0 < \alpha < 30^\circ, \mu = 60^\circ$$

Mode 4: 6 and 7 valve conduction

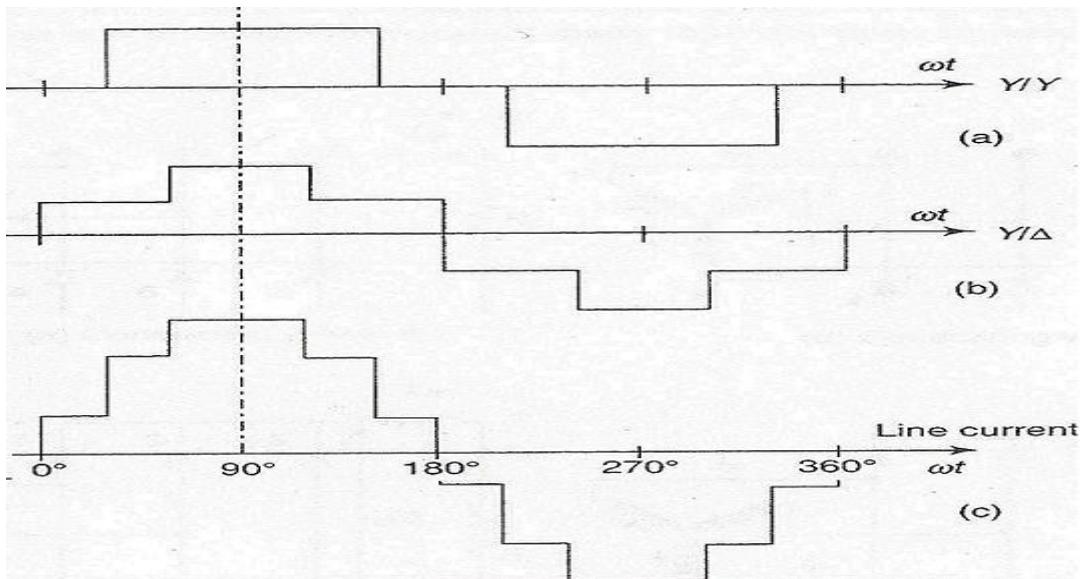
$$60^\circ < \mu < 90^\circ$$

Mode 5: 7 and 8 valve conduction

$$90^\circ < \mu < 120^\circ$$

The second mode is a continuation of the first and similarly fifth is a continuation of the fourth.

The equivalent circuit of the twelve pulse converter is the series combination of the equivalent circuits for the two bridges. This is because the two bridges are connected in series on the DC side and in parallel on the AC side. The current waveforms in the primary winding of the star/star and star/delta connected transformers and the line current injected into the converter bus are shown.



Questions

- 1) What is the need for interconnection of systems? Explain the merits of connecting HVAC systems by HVDC tie-lines?
- 2) (a) Discuss the different factors that favor HVDC transmission systems over EHVAC transmission over long distances.
 - (b) What are the different HVDC links normally adopted?
- 3) (a) With the help of a neat schematic diagram of a typical HVDC converter station explain the functions of various components available.
 - (b) What are the applications and merits of HVDC transmission system?
- 4) (a) Explain for what reasons as a system planner, you consider the applications of HVDC in India?

(b) Compare HVDC transmission system with AC system in all aspects.

5) For a 3-Φ, 6 pulse Graetz's circuit, draw the timing diagram considering overlap angle is less than 60° and without overlap for the following:

- (a) Voltage across load
- (b) Voltage across any two pair of conduction values

6) Explain the operation of a 12 pulse bridge rectifier with the help of circuit diagram, voltage & current waveforms.

7) (a) Clearly explain how harmonics are produced and obtain the expression for rms value of the fundamental component of the current.

- (b) Obtain a relation between firing angle and power factor angle in a 3-Φ bridge rectifier.

8) Derive the expression for average DC voltages of a six pulse bridge converter, considering gate control and source reactance.

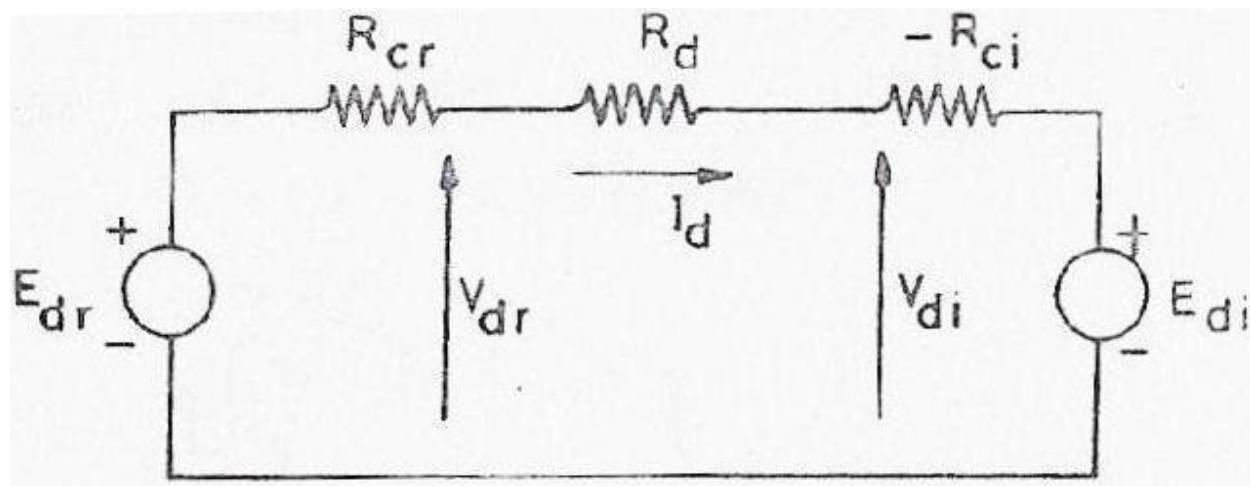
9) What is the reason for using star-star and star-delta transformer configurations for 12 pulse converter? Derive an equation for primary current using fourier analysis.

UNIT-III: CONTROL OF HVDC CONVERTER SYSTEMS

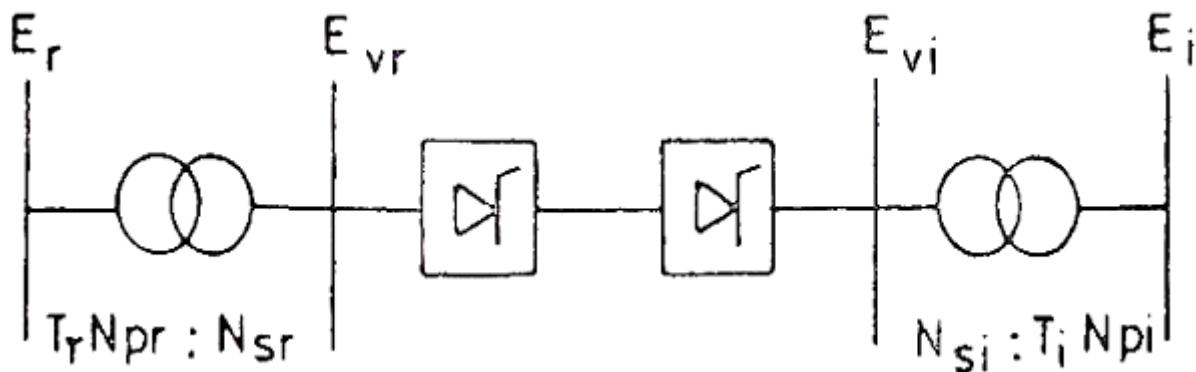
The major advantage of a HVDC link is rapid controllability of transmitted power through the control of firing angles of the converters. Modern converter controls are not only fast, but also very reliable and they are used for protection against line and converter faults.

Principles of DC Link Control

The control of power in a DC link can be achieved through the control of current or voltage. From minimization of loss considerations, we need to maintain constant voltage in the link and adjust the current to meet the required power.



Consider the steady state equivalent circuit of a two terminal DC link. This is based on the assumption that all the series connected bridges in both poles of a converter station are identical and have the same delay angles. Also the number of series connected bridges (n_b) in both stations (rectifier and inverter) are the same.



The voltage sources E_{dr} and E_{di} are defined by

$$E_{dr} = (3\sqrt{2}/\pi) n_b E_{vr} \cos \alpha_r \quad \text{--- (1)}$$

$$E_{di} = (3\sqrt{2}/\pi) n_b E_{vi} \cos \gamma_i \quad \text{--- (2)}$$

where E_{vr} and E_{vi} are the line to line voltages in the valve side windings of the rectifier and inverter transformer respectively. From the above figure these voltages can be obtained by

$$E_{vr} = \frac{N_{sr}E_r}{N_{pr}T_r} , \quad E_{vi} = \frac{N_{si}E_i}{N_{pi}T_i} \quad \text{---- (3)}$$

where E_r and E_i are the AC (line to line) voltages of the converter buses on the rectifier and inverter side. T_r and T_i are the OFF-nominal tap ratios on the rectifier and inverter side.

Combining equations (1), (2) and (3),

$$E_{dr} = (A_r E_r / T_r) \cos \alpha_r \quad \text{---- (4)}$$

$$E_{di} = (A_i E_i / T_i) \cos \gamma_i \quad \text{---- (5)}$$

where A_r and A_i are constants.

The steady-state current I_d in the DC link is obtained as

$$I_d = \frac{(E_{dr} - E_{di})}{R_{cr} + R_d - R_{ci}}$$

Substituting equations (4) and (5) in the above equation, we get

$$I_d = \frac{(A_r E_r / T_r) \cos \alpha_r - (A_i E_i / T_i) \cos \gamma_i}{R_{cr} + R_d - R_{ci}}$$

The control variables in the above equation are T_r , T_i and α_r , β_i . However, for maintaining safe commutation margin, it is convenient to consider γ_i as control variable instead of β_i .

As the denominator in the final equation is small, even small changes in the voltage magnitude E_r or E_i can result in large changes in the DC current, the control variables are held constant. As the voltage changes can be sudden, it is obvious that manual control of converter angles is not feasible. Hence, direct and fast control of current by varying α_r or γ_r in response to a feedback signal is essential.

While there is a need to maintain a minimum extinction angle of the inverter to avoid commutation failure, it is economical to operate the inverter at Constant Extinction Angle (CEA) which is slightly above the absolute minimum required for the commutation margin. This results in reduced costs of the inverter stations, reduced converter losses and reactive power consumption. However, the main drawback of CEA control is the negative resistance characteristics of the converter which makes it difficult to operate stably when the AC system is weak (low short-circuit ratios). Constant DC Voltage (CDCV) control or Constant AC Voltage (CACV) control are the alternatives that could be used at the inverter.

Under normal conditions, the rectifier operates at Constant Current (CC) control and the inverter at the CEA control.

The power reversal in the link can take place by the reversal of the DC voltage. This is done by increasing the delay angle at the station initially operating as a rectifier, while reducing the delay angle at the station initially operating as the inverter. Thus, it is necessary to provide both CEA and CC controllers at both terminals.

The feedback control of power in a DC link is not desirable because

- 1) At low DC voltages, the current required is excessive to maintain the required level of power. This can be counterproductive because of the excessive requirements of the reactive power, which depresses voltage further.
- 2) The constant power characteristic contributes to negative damping and degrades dynamic stability.

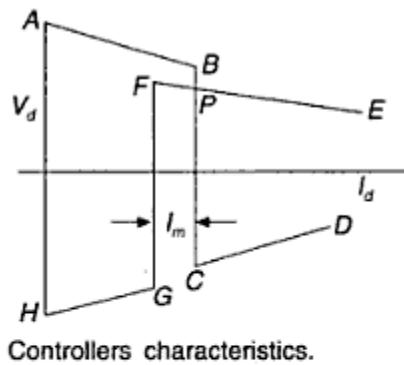
Converter Control Characteristics

Basic Characteristics:

The intersection of the two characteristics (point A) determines the mode of operation- Station I operating as rectifier with constant current control and station II operating at constant (minimum) extinction angle.

There can be three modes of operation of the link (for the same direction of power flow) depending on the ceiling voltage of the rectifier which determines the point of intersection of the two characteristics which are defined below

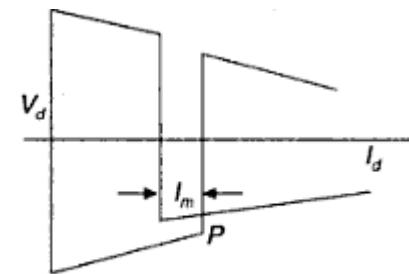
- 1) CC at rectifier and CEA at inverter (operating point A) which is the normal mode of operation.
- 2) With slight dip in the AC voltage, the point of intersection drifts to C which implies minimum α at rectifier and minimum γ at the inverter.
- 3) With lower AC voltage at the rectifier, the mode of operation shifts to point B which implies CC at the inverter with minimum α at the rectifier.



Types of Station Control Characteristics

Station-I	Station-II	Controller type
AB	HG	Minimum α
BC	GF	Constant current
CD	EF	CEA (minimum γ)

The characteristic AB has generally more negative slope than characteristic FE because the slope of AB is due to the combined resistance of $(R_d + R_{cr})$ while is the slope of FE is due to R_{ci} .



Power reversal controllers characteristics

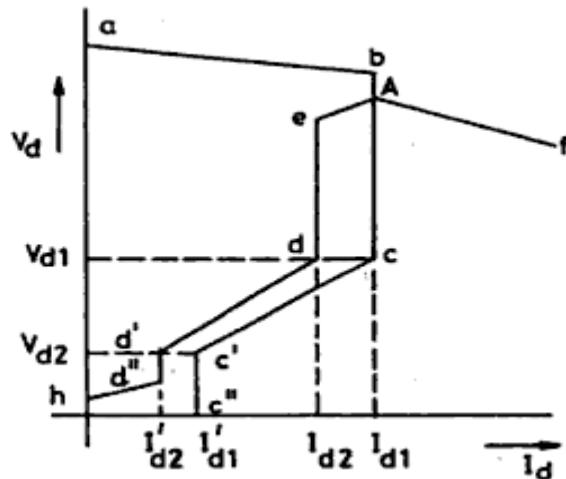
The above figure shows the control characteristics for negative current margin I_m (or where the current reference of station II is larger than that of station I). The operating point shifts now to D which implies power reversal with station I (now acting as inverter) operating with minimum CEA control while station II operating with CC control.

This shows the importance of maintaining the correct sign of the current margin to avoid inadvertent power reversal. The maintenance of proper current margin requires adequate telecommunication channel for rapid transmission of the current or power order.

Voltage Dependent Current Limit:

The low voltage in the DC link is mainly due to the faults in the AC system on the rectifier or inverter side. The low AC voltage due to faults on the inverter side can result in

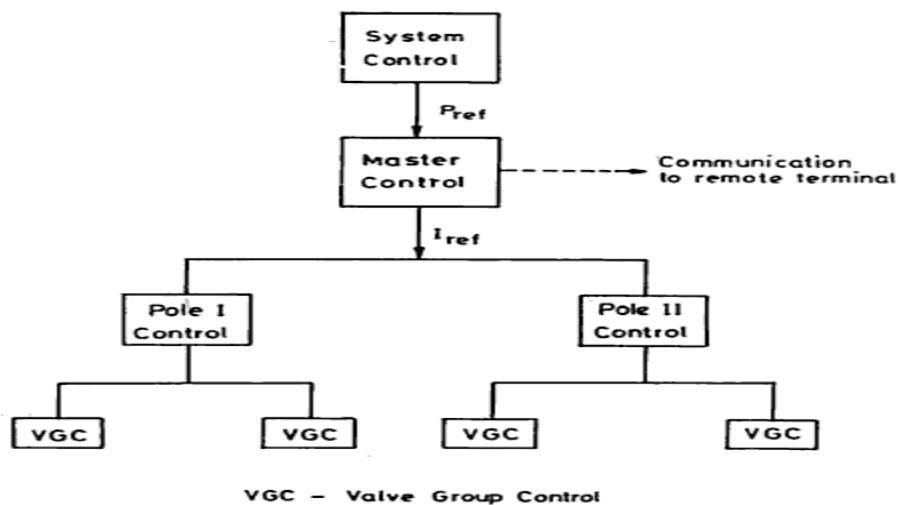
persistent commutation failure because of the increase of the overlap angle. In such cases, it is necessary to reduce the DC current in the link until the conditions that led to the reduced DC voltage are relieved. Also the reduction of current relieves those valves in the inverter which are overstressed due to continuous current flow in them.



If the low voltage is due to faults on the rectifier side AC system, the inverter has to operate at very low power factor causing excessive consumption of reactive power which is also undesirable. Thus, it becomes useful to modify the control characteristics to include voltage dependent current limits. The figure above shown shows current error characteristics to stabilize the mode when operating with DC current between I_{d1} and I_{d2} . The characteristic cc^1 and cc^2 show the limitation of current due to the reduction in voltage.

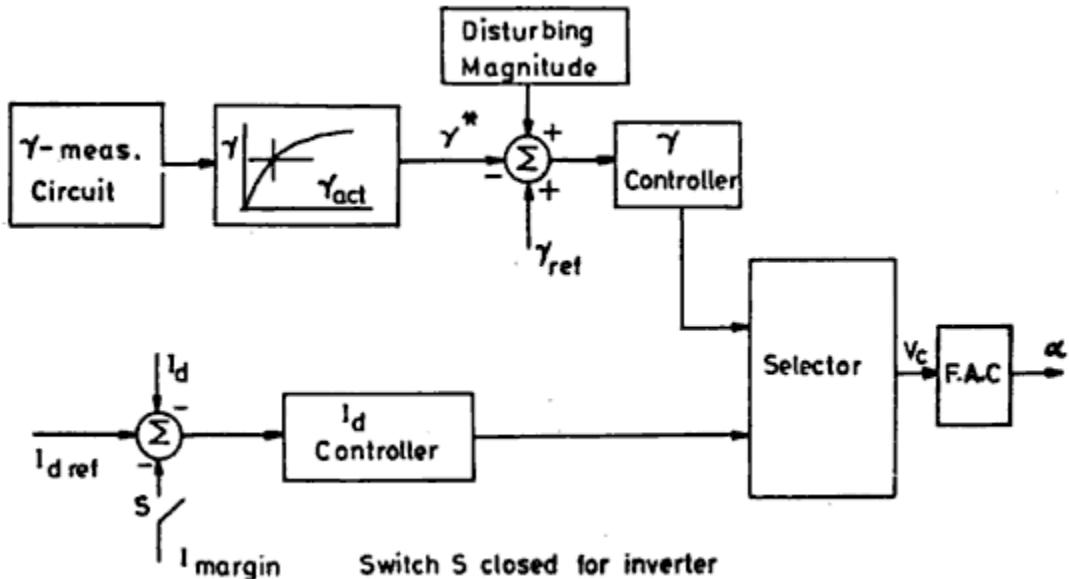
System Control Hierarchy

The control function required for the HVDC link is performed using the hierarchical control structure.



The master controller for a bipole is located at one of the terminals and is provided with the power order (P_{ref}) from the system controller (from energy control centre). It also has other information such as AC voltage at the converter bus, DC voltage etc. The master controller transmits the current order (I_{ref}) to the pole control units which in turn provide a firing angle order to the individual valve groups (converters). The valve group or converter control also oversees valve monitoring and firing logic through the optical interface. It also includes bypass pair selection logic, commutation failure protection, tap changer control, converter start/stop sequences, margin switching and valve protection circuits.

The pole control incorporates pole protection, DC line protection and optional converter paralleling and deparalleling sequences. The master controller which oversees the complete bipole includes the functions of frequency control, power modulation, AC voltage and reactive power control and torsional frequency damping control.



The current or extinction angle controller generates a control signal V_c which is related to the firing angle required. The firing angle controller generates gate pulses in response to the control signal V_c . The selector picks the smaller of the α determined by the current and CEA controllers.

Firing Angle Control

The operation of CC and CEA controllers is closely linked with the method of generation of gate pulses for the valves in a converter. The requirements for the firing pulse generation of HVDC valves are

1. The firing instant for all the valves are determined at ground potential and the firing signals sent to individual thyristors by light signals through fibre-optic cables. The required gate power is made available at the potential of individual thyristor.
2. While a single pulse is adequate to turn-on a thyristor, the gate pulse generated must send a pulse whenever required, if the particular valve is to be kept in a conducting state.

The two basic firing schemes are

1. Individual Phase Control (IPC)
2. Equidistant Pulse Control (EPC)

Individual Phase Control (IPC)

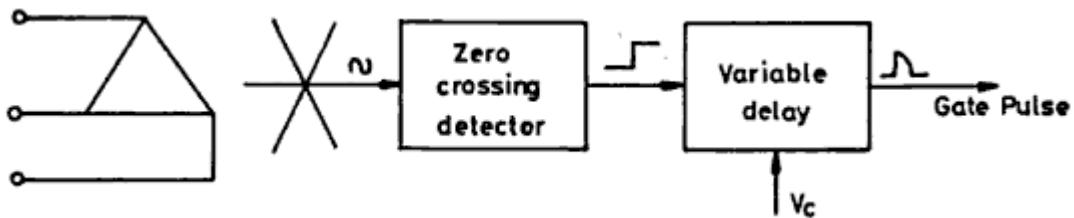
This was used in the early HVDC projects. The main feature of this scheme is that the firing pulse generation for each phase (or valve) is independent of each other and the firing pulses are rigidly synchronized with commutation voltages.

There are two ways in which this can be achieved

1. Constant α Control
2. Inverse Cosine Control

Constant α Control

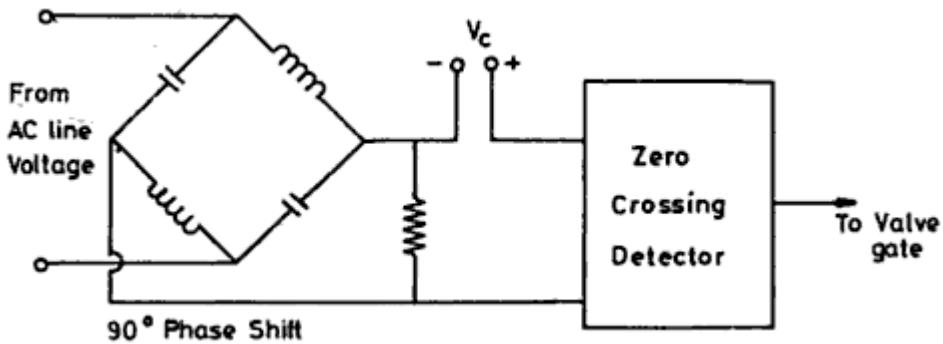
Six timing (commutation) voltages are derived from the converter AC bus via voltage transformers and the six gate pulses are generated at nominally identical delay times subsequent to the respective voltage zero crossings. The instant of zero crossing of a particular commutation voltage corresponds to $\alpha = 0^\circ$ for that valve.



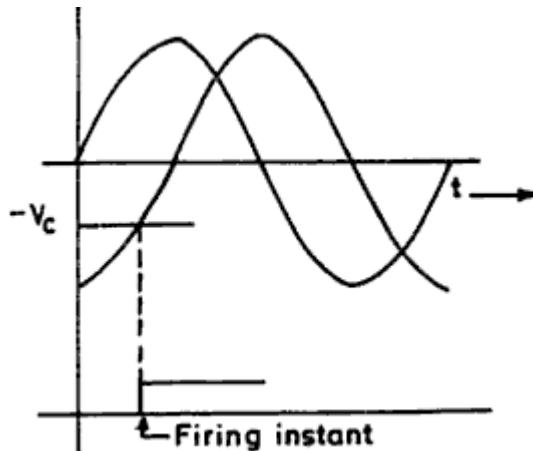
The delays are produced by independent delay circuits and controlled by a common control voltage V derived from the current controllers.

Inverse Cosine Control

The six timing voltages (obtained as in constant α control) are each phase shifted by 90° and added separately to a common control voltage V .



The zero crossing of the sum of the two voltages initiates the firing pulse for the particular valve is considered. The delay angle α is nominally proportional to the inverse cosine of the control voltage. It also depends on the AC system voltage amplitude and shape.



The main advantage of this scheme is that the average DC voltage across the bridge varies linearly with the control voltage V_c .

Drawbacks of IPC Scheme

The major drawback of IPC scheme is the aggravation of the harmonic stability problem that was encountered particularly in systems with low short circuit ratios (less than 4). The harmonic instability, unlike instability in control systems, is a problem that is characterized by magnification of noncharacteristic harmonics in steady-state.

This is mainly due to the fact that any distortion in the system voltage leads to perturbations in the zero crossings which affect the instants of firing pulses in IPC scheme. This implies that even when the fundamental frequency voltage components are balanced, the firing

pulses are not equidistant in steady-state. This in turn leads to the generation of noncharacteristic harmonics (harmonics of order $h \neq np \pm 1$) in the AC current which can amplify the harmonic content of the AC voltage at the converter bus. The problem of harmonic instability can be overcome by the following measures

1. Through the provision of synchronous condensers or additional filters for filtering out noncharacteristic harmonics.
2. Use of filters in control circuit to filter out noncharacteristic harmonics in the commutation voltages.
3. The use of firing angle control independent of the zero crossings of the AC voltages. This is the most attractive solution and leads to the Equidistant Pulse Firing scheme.

Equidistant Pulse Control (EPC)

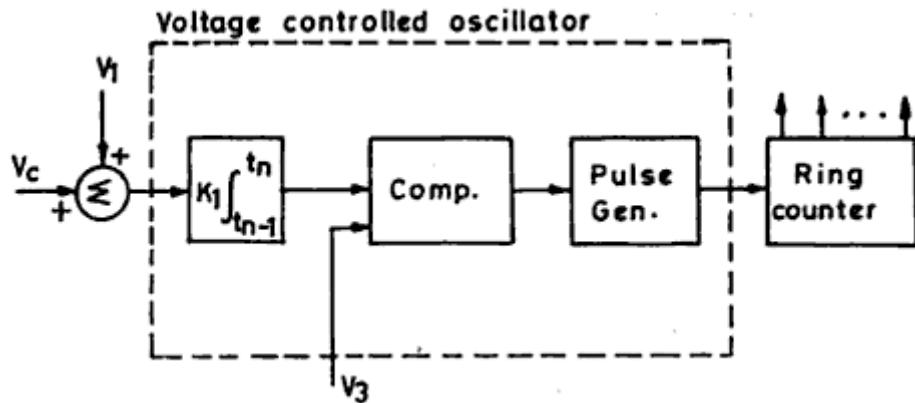
The firing pulses are generated in steady-state at equal intervals of $1/pf$, through a ring counter. This control scheme uses a phase locked oscillator to generate the firing pulses. There are three variations of the EPC scheme

1. Pulse Frequency Control (PFC)
2. Pulse Period Control
3. Pulse Phase Control (PPC)

Pulse Frequency Control (PFC)

A Voltage Controlled Oscillator (VCO) is used, the frequency of which is determined by the control voltage V_c which is related to the error in the quantity (current, extinction angle or DC voltage) being regulated. The frequency in steady-state operation is equal to pf_0 where f_0 is the nominal frequency of the AC system. PFC system has an integral characteristic and has to be used along with a feedback control system for stabilization.

The Voltage Controlled Oscillator (VCO) consists of an integrator, comparator and a pulse generator.



The output pulses of the generator drive the ring counter and also reset the integrator. The instant (t_n) of the firing pulse is determined by

$$\int_{t_{n-1}}^{t_n} K_1(V_c + V_1) dt = V_3$$

where V_1 is a bias (constant) voltage and V_3 is proportional to the system period.

In steady-state, $V_c = 0$, and from the above equation, we get

$$K_1 V_1 (t_n - t_{n-1}) = V_3$$

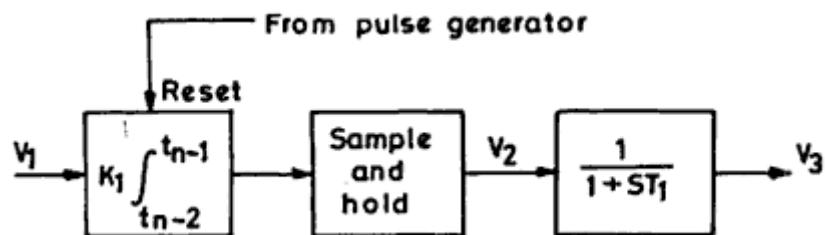
Since, $t_n - t_{n-1} = 1/pf_0$

in steady-state, the gain K_1 of the integrator is chosen as

$$K_1 = p f_0 V_3 / V_1$$

The circuit does not incorporate frequency correction (when the system frequency deviates from f_o). The frequency correction is obtained by deriving V_3 as

$$V_3 = V_2 / (1 + ST_1), \quad V_2 = K_1 V_1 (t_{n-1} - t_{n-2})$$



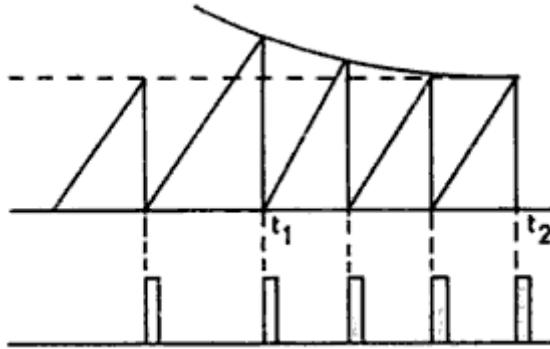
Pulse Period Control

It is similar to PFC except for the way in which the control voltage V_c is handled. The structure of the controller is the same, however, V_c is now summed with V_3 instead of V_1 . Thus, the instant t_n of the pulse generation is

$$\int_{t_{n-1}}^{t_n} K_1 V_1 dt = V_3 + V_c$$

$$K_1 V_1 (t_n - t_{n-1}) = V_3 + V_c$$

With $V_c = 0$, the interval between consecutive pulses, in steady-state, is exactly equal to $1/pf_o$.



The frequency correction in this scheme is obtained by either updating V_1 in response to the system frequency variation or including another integrator in the CC or CEA controller.

Pulse Phase Control (PPC)

An analog circuit is configured to generate firing pulses according to the following equation

$$\int_{t_{n-1}}^{t_n} K_1 V_1 dt = V_{cn} - V_{c(n-1)} + V_3$$

where V_{cn} and $V_{c(n-1)}$ are the control voltages at the instants t_n and t_{n-1} respectively.

For proportional current control, the steady-state can be reached when the error of V_c is constant.

The major advantages claimed for PPC over PFC are (i) easy inclusion of α limits by limiting V_c as in IPC and (ii) linearization of control characteristic by including an inverse cosine function block after the current controller. Limits can also be incorporated into PFC or pulse period control system.

Drawbacks of EPC Scheme

EPC Scheme has replaced IPC Scheme in modern HVDC projects; it has certain limitations which are

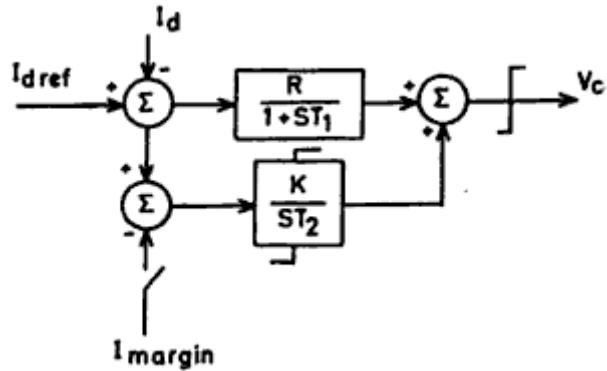
1. Under balanced voltage conditions, EPC results in less DC voltage compared to IPC. Unbalance in the voltage results from single phase to ground fault in the AC system

which may persist for over 10 cycles due to stuck breakers. Under such conditions, it is desirable to maximize DC power transfer in the link which calls for IPC.

2. EPC Scheme also results in higher negative damping contribution to torsional oscillations when HVDC is the major transmission link from a thermal station.

Current and Extinction Angle Control

The current controller is invariably of feedback type which is of PI type.



The extinction angle controller can be of predictive type or feedback type with IPC control. The predictive controller is considered to be less prone to commutation failure and was used in early schemes. The feedback control with PFC type of Equidistant Pulse Control overcomes the problems associated with IPC.

The extinction angle, as opposed to current, is a discrete variable and it was felt the feedback control of gamma is slower than the predictive type. The firing pulse generation is based on the following equation

$$0 = \int_{-\pi+\delta_{n-1}}^{\omega t_n} e_{cj} d(\omega t) + 2X_c I_d$$

where e_{cj} is the commutation voltage across valve j and t_n is the instant of its firing.

In general, the prediction of firing angle is based on the equation

$$B_j = \gamma_{ref} + \mu_j$$

where μ_j is the overlap angle of valve j, which is to be predicted based on the current knowledge of the commutation voltage and DC current.

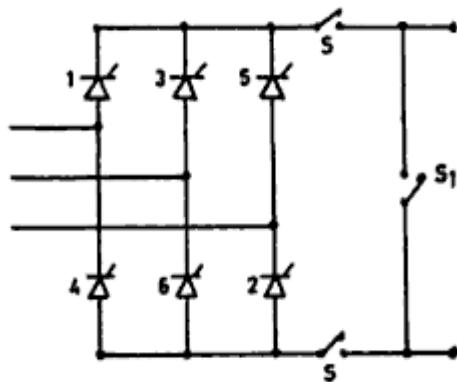
Under large disturbances such as a sudden dip in the AC voltage, signals derived from the derivative of voltage or DC current aid the advancing of delay angle for fast recovery from commutation failures.

Starting and Stopping of DC Link

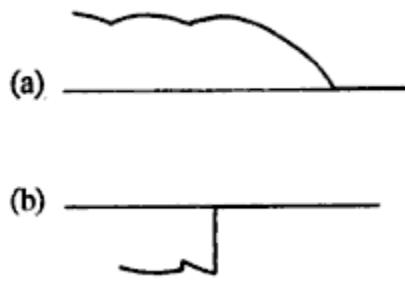
Energization and Deenergization of a Bridge:

Consider N series connected bridges at a converter station. If one of the bridges is to be taken out of service, there is need to not only block, but bypass the bridge. This is because of the fact that just blocking the pulses does not extinguish the current in the pair of valves that are left conducting at the time of blocking. The continued conduction of this pair injects AC voltage into the link which can give rise to current and voltage oscillations due to lightly damped oscillatory circuit in the link formed by smoothing reactor and the line capacitance. The transformer feeding the bridge is also subjected to DC magnetization when DC current continues to flow through the secondary windings.

The bypassing of the bridge can be done with the help of a separate bypass valve or by activating a bypass pair in the bridge (two valves in the same arm of the bridge). The bypass valve was used with mercury arc valves where the possibility of arc backs makes it impractical to use bypass pairs. With thyristor valves, the use of bypass pair is the practice as it saves the cost of an extra valve.



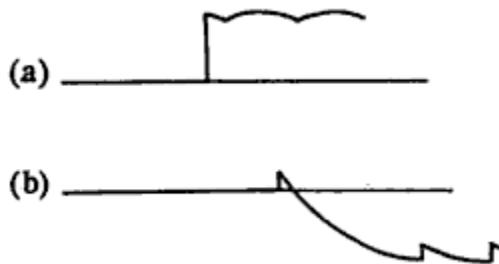
With the selection of bypass pair 1 and 4, the commutation from valve 2 to 4 is there, but the commutation from valve 3 to valve 5 is prevented. In the case of a predetermined choice of the bypass path, the time lapse between the blocking command and the current transfer to bypass path can vary from 60° and 180° for a rectifier bridge. In the inverter, there is no time lag involved in the activation of the bypass pair. The voltage waveforms for the rectifier and inverter during de-energisation are shown below where the overlap is neglected.



The current from bypass pair is shunted to a mechanical switch S_1 . With the aid of the isolators S , the bridge can be isolated. The isolator pair S and switch S_1 are interlocked such that one or both are always closed.

The energisation of a blocked bridge is done in two stages. The current is first diverted from S_1 to the bypass pair. For this to happen S_1 must generate the required arc voltage and to minimize this voltage, the circuit inductance must be small. In case the bypass pair fails to take over the current, S_1 must close automatically if the current in that does not become zero after a predetermined time interval. AC breakers with sufficient arc voltage, but with reduced breaking capacity are used as switch S_1 .

In the second stage of energisation, the current is diverted from the bypass pair. For the rectifier, this can take place instantaneously neglecting overlap. The voltage waveforms for this case are shown below.



Start-Up of DC Link:

There are two different start-up procedures depending upon whether the converter firing controller provides a short gate pulse or long gate pulse. The long gate pulse lasts nearly 120° , the average conduction period of a valve.

Start-up with long pulse firing:

1. Deblock inverter at about $\gamma = 90^\circ$
2. Deblock rectifier at $\alpha = 85^\circ$ to establish low direct current
3. Ramp up voltage by inverter control and the current by rectifier control.

Start-up with short pulse firing:

1. Open bypass switch at one terminal
2. Deblock that terminal and load to minimum current in the rectifier mode
3. Open bypass switch at the second terminal and commutate current to the bypass pair
4. Start the second terminal also in the rectifier mode
5. The inverter terminal is put into the inversion mode
6. Ramp up voltage and current.

The voltage is raised before raising the current. This permits the insulation of the line to be checked before raising the power. The ramping of power avoids stresses on the generator shaft. The switching surges in the line are also reduced.

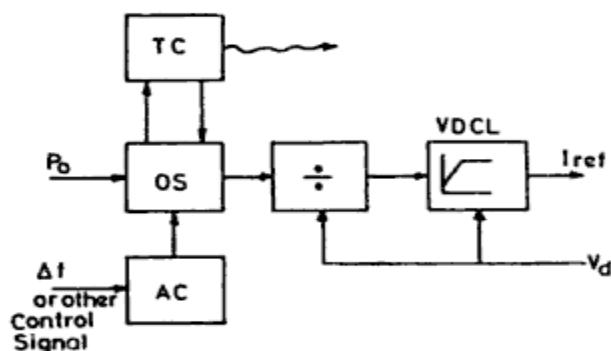
The required power ramping rate depends on the strength of the AC system. Weaker systems require fast restoration of DC power for maintaining transient stability.

Power Control

The current order is obtained as the quantity derived from the power order by dividing it by the direct voltage. The limits on the current order are modified by the voltage dependent current order limiter (VDCOL). The objective of VDCOL is to prevent individual thyristors from carrying full current for long periods during commutation failures.

By providing both converter stations with dividing circuits and transmitting the power order from the leading station in which the power order is set to the trailing station, the fastest response to the DC line voltage changes is obtained without undue communication requirement.

The figure below shows the basic power controller used.



TC-Telecommunication equipment
OS-Order Setting unit

VDCL-Voltage dependent current limiter

When the DC line resistance is large and varies considerably e.g., when the overhead line is very long and exposed to large temperature variations, the DC line voltage drop cannot be compensated individually in the two stations. This problem can be solved by using a current order calculated in one substation only and transmitting its output to the other substation.

Questions:

- 1) Write detailed notes on the following
 - (a) Predictive commutation margin control
 - (b) Equidistant firing control.
- 2) (a) Differentiate between the two start-up procedures based upon the pulse.
 (b) Describe about starting and stopping of DC link.
- 3) (a) Explain with neat sketch, constant extinction angle control.
 (b) What is meant by current margin between two stations in a HVDC link? Why is the inverter station, operated as a constant voltage controller under normal conditions?
- 4) Enumerate the relative merits and demerits of constant current control and constant voltage control of HVDC link.
- 5) (a) Explain the necessity of "VDCOL" control in a HVDC link with the help of VI characteristics..
 (b) Explain the procedure of Energization and Deenergization of a converter bridge.
- 6) (a) Draw the complete converter control characteristics and explain the principle of power control in a DC link.
 (b) Explain Inverse cosine control scheme for firing pulse generations.
- 7) (a) Explain pulse frequency control scheme for firing pulse generation and discuss its drawbacks.
 (b) Explain clearly the procedure for start up of a DC link.
- 8) Explain the individual characteristics of a Rectifier and an Inverter with sketches.
- 9) With block diagram, discuss the principle of operation of a basic power controller.
- 10) Write short notes on the following:

(a) Constant Alpha control	(b) Inverse cosine control.
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- 11) Explain the drawbacks in Individual phase control and equidistant pulse control schemes used in HVDC projects.

Introduction, generation of harmonics, AC & DC Filters, Reactive power requirements at steady state, sources of reactive power, static VAR systems

Electrical energy transmitted through AC transmission or DC transmission is to be delivered at the consumer's terminals at specified voltage level of constant magnitude without deviation from the ideal waveform.

An HVDC transmission system generates harmonic currents on the AC side and harmonic voltages on the DC side during operation. The harmonic currents generated at the AC bus of the converter get transmitted to the AC network and then cause the following adverse effects.

- a) Heating of the equipments connected.
- b) Instability of converter control.
- c) Generates telephone and radio interference in adjacent communication lines, thereby inducing harmonic noise.
- d) Harmonics can lead to generation of overvoltages due to resonance when filter circuits are employed.

An HVDC transmission system consists of a rectifier and an inverter whose operation generates harmonics on AC and DC side of the converter. The three distinct sources of harmonics in HVDC systems are

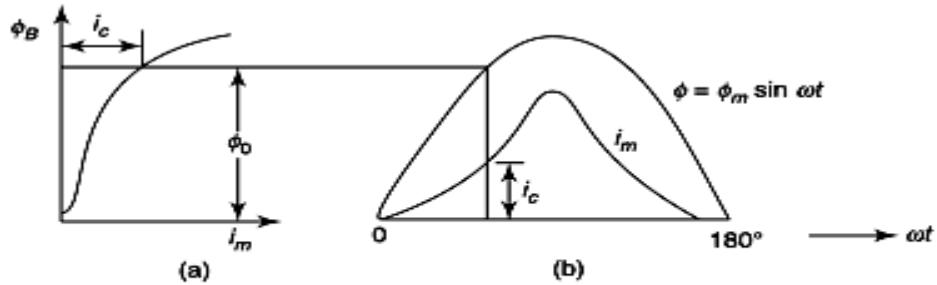
- 1) Transformer.
- 2) AC Generator.
- 3) Converter along with its control devices.

Transformer as source of harmonics

Transformers can be considered as source of harmonic voltages, which arise from magnetic distortion and magnetic saturation due to the presence of a DC component in its secondary. The magnitude of these harmonics depends upon the operating flux density. Converter transformers are usually operated at high flux densities than conventional 3-phase transformers, and therefore the possibility of generation of harmonics is more.

Although the waveform is usually good, an AC generator may be regarded as a source of balanced harmonics because of non-uniform distribution of flux on the armature windings.

The converter which forms the basic unit in HVDC transmission imposes changes of impedances in the current.

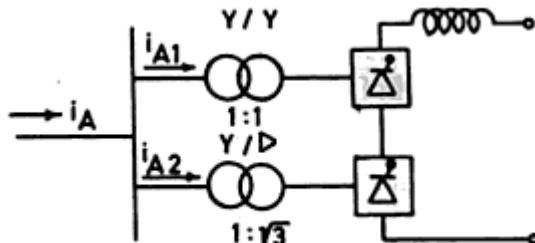


Transformer magnetisation (without hysteresis)
 (a) Magnetisation curve (b) Flux and magnetisation current waveforms

When hysteresis effect is considered, then the non-sinusoidal magnetizing current waveform is no longer symmetrical which is mainly caused by triple n harmonics and particularly the third harmonic. Thus, in order to maintain a reasonable sinusoidal voltage supply, it is necessary to supply a path for triple n harmonics which is achieved by the use of delta-connected windings.

Harmonics due to Converters

A 12-pulse connection consists of two 6-pulse groups. One group having Y-Y connected converter transformer with 1:1 turns ratio and the other group having Y-Δ converter transformer bank with $1:\sqrt{3}$ turns ratio.



Schematic Diagram of a 12 Pulse Converter Unit

Generation of Harmonics

The harmonics which are generated are of two types.

- (i) Characteristic harmonics.
- (ii) Non- characteristic harmonics.

Characteristic Harmonics

The characteristic harmonics are harmonics which are always present even under ideal operation.

In the converter analysis, the DC current is assumed to be constant. But in AC current the harmonics exist which are of the order of

$$h = np \pm 1$$

and in DC current it is of the order of

$$h = np$$

where n is any integer and p is pulse number.

Neglecting overlap, primary currents of Y-Y and Y- Δ connection of the transformer are considered taking the origin symmetrical where

$$\begin{aligned}
 i &= I_d \text{ for } -\pi/3 \leq \omega t \leq \pi/3 \\
 &= 0 \text{ for } \pi/3 \leq \omega t \leq 2\pi/3 \text{ and} \\
 &\quad -\pi/3 \leq \omega t \leq -2\pi/3 \\
 &= -I_d \text{ for } -2\pi/3 \leq \omega t \leq -\pi \text{ and} \\
 &\quad 2\pi/3 \leq \omega t \leq \pi
 \end{aligned}
 \quad \left. \begin{array}{l} \text{for Y-Y connection} \\ \text{converter} \\ \text{transformer} \end{array} \right\}$$

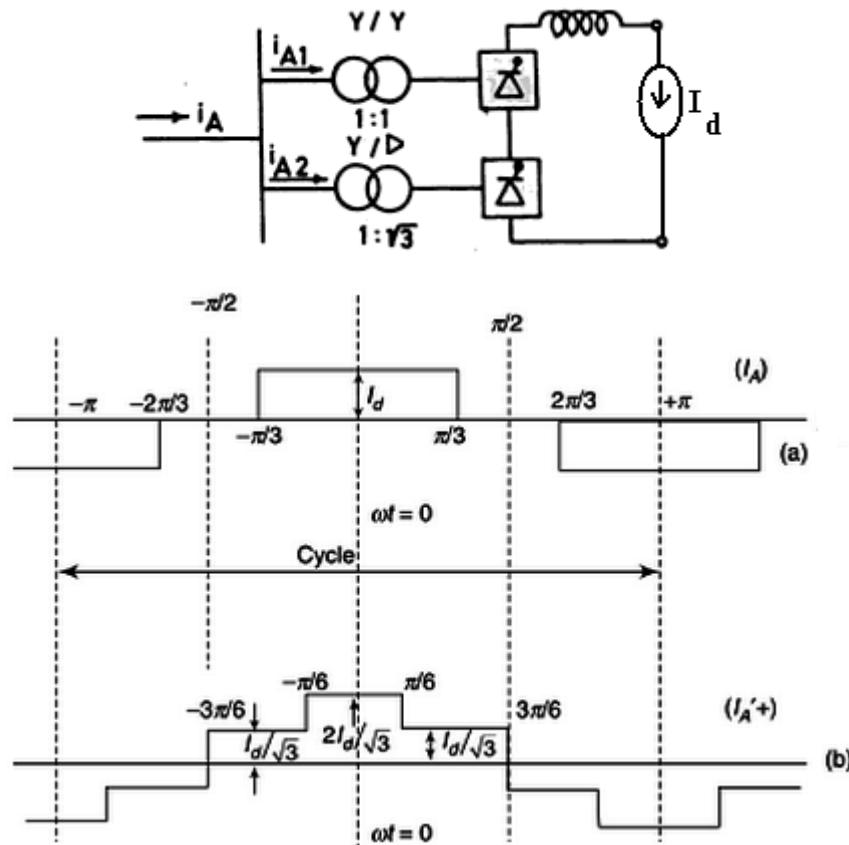


Figure (a): Phase current on primary side of Y-Y connection converter transformer

Figure (b): Phase current on primary side of Y- Δ connection converter transformer

For convenience, the ordinate axis (corresponding to $\omega t = 0$) is chosen such that the waveform has even symmetry. So, generally, by fourier series

$$f(t) = \frac{1}{2}a_0 + \sum_{n=0}^{\infty} a_n \cos n\omega t + \sum_{n=0}^{\infty} b_n \sin n\omega t$$

As positive and negative half cycle cancel each other, so $a_0 = 0$ and as it is (waveform is) even symmetry, so $b_n = 0$ due to which $f(t)$ becomes

$$f(t) = \sum_{n=0}^{\infty} a_n \cos n\omega t \text{ (or) } \sum_n a_n \cos n\omega t$$

$$\text{Therefore, } i_{A_1} = \sum_n a_{n_1} \cos n\omega t$$

$$\text{where, } a_{n_1} = \frac{2}{T} \int_0^{\text{PeriodOfConduction}} f(t) dt$$

Here total time period is $T = \pi$ and period of conduction is $\pi/3$

So,

$$a_{n_1} = 2X \frac{2}{\pi} \int_0^{\pi/3} I_d \cos n\omega t d(\omega t)$$

(Here as it is symmetry)

$$a_{n_1} = \frac{4I_d}{\pi} \int_0^{\pi/3} \cos n\omega t d(\omega t) = \frac{4I_d}{\pi} \left(\frac{\sin n\omega t}{n} \right)_0^{\pi/3}$$

$$a_{n_1} = \frac{4I_d}{n\pi} \left(\sin n \frac{\pi}{3} \right)$$

For triplen harmonics, $a_{n_1} = 0$

Questions

- 1) Derive the relationship between pulse conversion and harmonics generated.
- 2) What are the various sources of harmonics generation in a HVDC line?
- 3) (a) Discuss the effect of pulse number and overlap angle on harmonics generated by HVDC converters.
 (b) Using fourier analysis show that the lowest order voltage harmonic present in Graetz circuit output voltage is six.
- 4) Analyze the harmonics in the AC current during 6-pulse and 12-pulse operations using fourier analysis. What orders of harmonics predominate in the current wave?

20) (a) Describe the method of compensation of reactive power in HVDC substation.
 (b) Draw simple single line schematics for each.

21) What is a Static VAR system? How many types of SVS schemes are present and what are they?

22) (a) Discuss about alternate converter control strategies for reactive power control.
 (b) Discuss how shunt capacitors can be used to meet reactive power requirement of a converter.

23) (a) Why Reactive power control is required for HVDC stations? Discuss about conventional control strategies for Reactive power control in HVDC link.
 (b) Discuss how reactive power requirement is met using synchronous condensers.

25) Write a note on the following sources of reactive power

(a) Synchronous condensers
 (b) Static VAR system

Design of AC Filters

1. Harmonic Distortion:

Harmonic Distortion is given by,

$$D = \frac{\sum_{n=2}^m I_n Z_n}{E_1} \times 100$$

where,

I_n – harmonic current injected

Z_n – harmonic impedance of the system

E_1 – fundamental component of line to neutral voltage

m – highest harmonic considered

Harmonic Distortion is also given by,

$$D_{RSS} = \frac{\left[\sum_{n=2}^m (I_n Z_n)^2 \right]^{1/2}}{E_1} \times 100$$

2. Telephone Influence Factor (TIF):

An index of possible telephone interference and is given by,

$$TIF = \frac{\left[\sum_{n=2}^m (I_n Z_n F_n)^2 \right]^{1/2}}{E_1}$$

where,

$$F_n = 5 n f_1 p_n$$

P_n is the c message weighting used by Bell Telephone Systems (BTS) and Edison Electric Institute (EEI) in USA. This weighting reflects the frequency dependent sensitivity of the human ear and has a maximum value at the frequency of 1000Hz.

3. Telephone Harmonic Form Factor (THFF):

It is similar to TIF and is given by,

$$F_n = (n f_1 / 800) W_n$$

where,

W_n – weight at the harmonic order n , defined by the Consultative Commission on Telephone and Telegraph Systems (CCITT).

TIF is used in USA.

THFF is popular in Europe.

4. IT Product:

In BTS-EEI system, there is another index called IT product and is defined by,

$$IT = \left[\sum_{n=2}^m (I_n F_n)^2 \right]^{1/2}$$

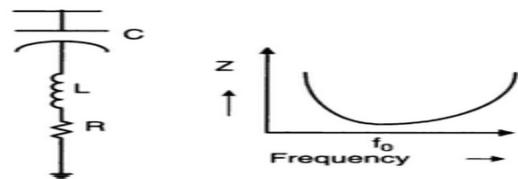
Types of AC Filters

The various types of filters that are used are

1. Single Tuned Filter
2. Double Tuned Filter
3. High Pass Filter
 - a) Second Order Filter
 - b) C Type Filter

Single Tuned Filter

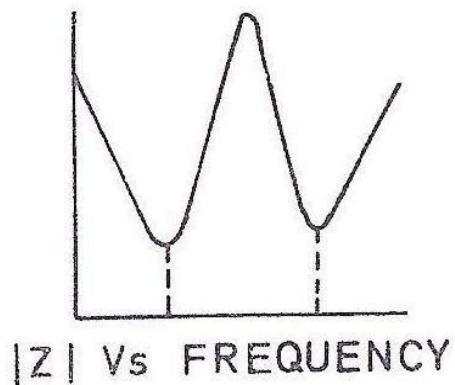
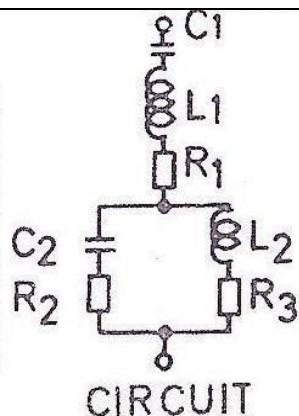
Single Tuned Filters are designed to filter out characteristic harmonics of single frequency.



Double Tuned Filter

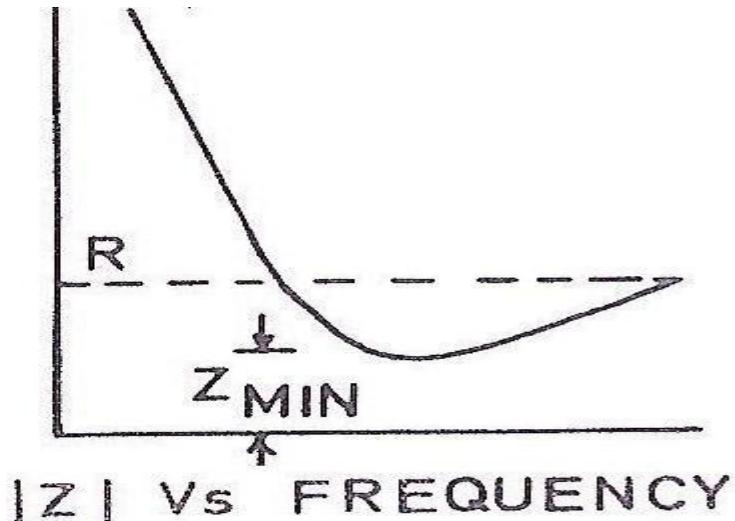
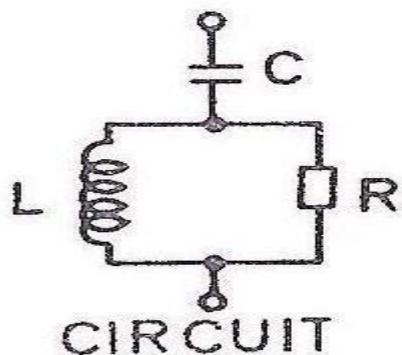
The Double Tuned Filters are used to filter out two discrete frequencies, instead of using two Single Tuned Filters. Their main disadvantages are

- i. only one inductor is subject to full line impulse voltage.
- ii. power loss at the fundamental frequency is considerably reduced.



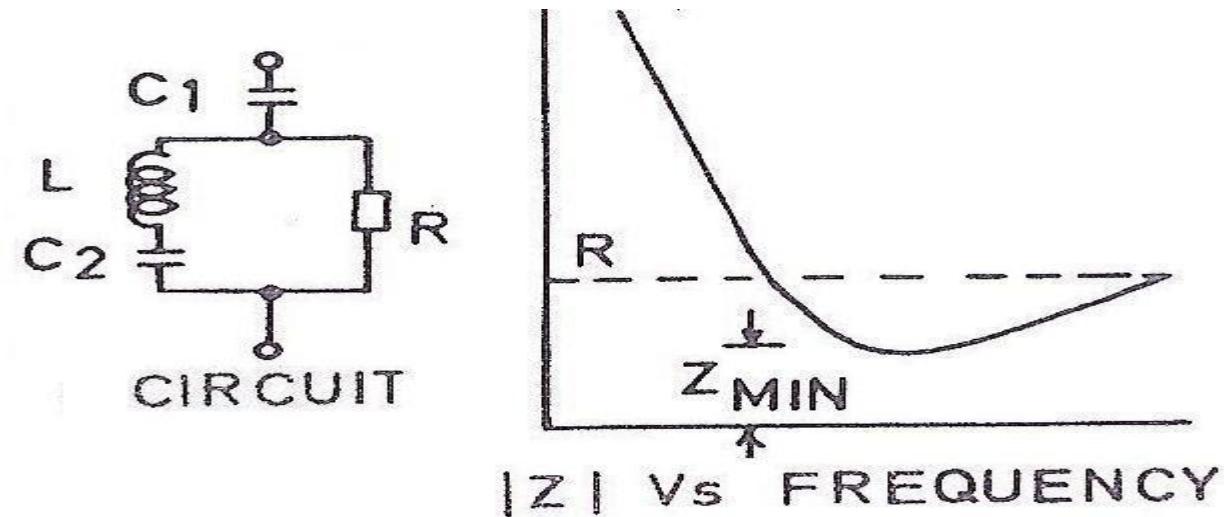
Second Order High Pass Filter

The Second Order High Pass Filters are designed to filter out higher harmonics.



High Pass C Type Filter

The losses at the fundamental frequency can be reduced by using a C Type Filter where capacitor C_2 is in series with inductor L , which provides a low impedance path to the fundamental component of current.



A converter system with 12 pulse converters has Double Tuned (or two Single Tuned) Filter banks to filter out 11th and 13th harmonics and a High Pass Filter bank to filter the rest of harmonics. Sometimes a third harmonic filter may be used to filter the non-characteristic harmonics of the 3rd order particularly with weak AC systems where some voltage unbalance is expected.

All filter branches appear capacitive at fundamental frequency and supply reactive power.

Design of Single Tuned Filter

The impedance Z_{Fh} of the single tuned filter at the harmonic order 'h' is given by

$$Z_{Fh} = R + j \left(h\omega L - \frac{1}{h\omega C} \right)$$

where ω is the fundamental frequency which can vary with the power system operating conditions.

A tuned filter is designed to filter a single harmonic of order h_r . If $h_r\omega = \omega_r$, then

$$Z_{Fh} = R = \frac{X_0}{Q} \text{ and is minimum.}$$

Since ω is variable and there could be errors in the tuning ($\omega_r \neq h_r \omega_n$ where ω_n is the nominal (rated) frequency), it is necessary to compute the impedance of the tuned filter as a function of the detuning parameter (δ) defined by

$$\delta = \frac{h_r \omega - \omega_r}{h_r \omega_n} = \frac{\omega}{\omega_n} - \frac{\omega_r}{h_r \omega_n}$$

Considering variations in the frequency (f), inductance (L) and capacitance (C),

$$\delta = 1 + \frac{\Delta f}{f_n} - \left[\left(1 + \frac{\Delta L}{L_n} \right) \left(1 + \frac{\Delta C}{C_n} \right) \right]^{1/2}$$

$$\delta = \frac{\Delta f}{f_n} + \frac{1}{2} \frac{\Delta L}{L_n} + \frac{1}{2} \frac{\Delta C}{C_n}$$

where L_n and C_n are the nominal values of L and C such that $h_r \omega_n = (L_n C_n)^{-1/2}$

The variation in C can be due to

- (i) error in the initial setting of C
- (ii) the variation in C due to the temperature dependence of the dielectric constant.

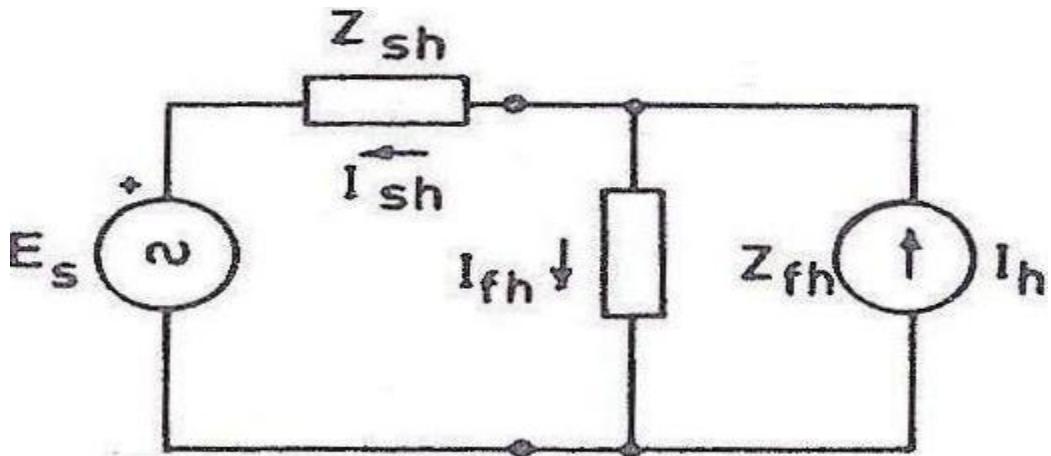
$$Z_{Fh} = R + jX_0 \left(\frac{\omega}{\omega_n} \frac{L}{L_n} - \frac{\omega_n}{\omega} \frac{C_n}{C} \right)$$

where

$$X_0 = h_r \omega_n L_n = \frac{1}{h_r \omega_n C_n}$$

The single tuned filters are designed to filter out characteristic harmonics of single frequency. The harmonic current in the filter is given by

$$I_{Fh} = \frac{I_h |Z_{Sh}|}{|Z_{Sh} + Z_{Fh}|}$$

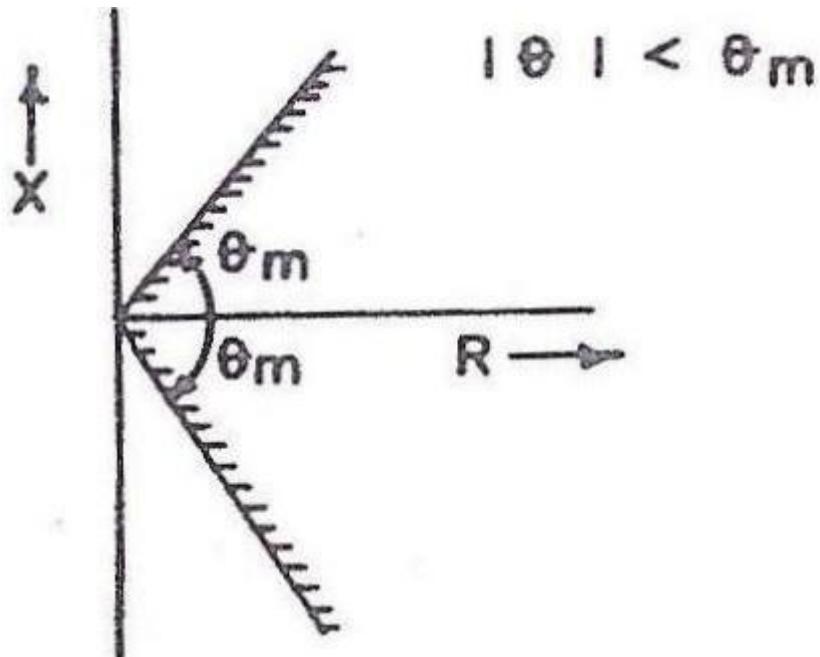


The harmonic voltage at the converter bus is

$$V_h = I_{Fh} |Z_{Fh}| = \frac{I_h}{|Y_{Fh} + Y_{Sh}|} = \frac{I_h}{|Y_h|}$$

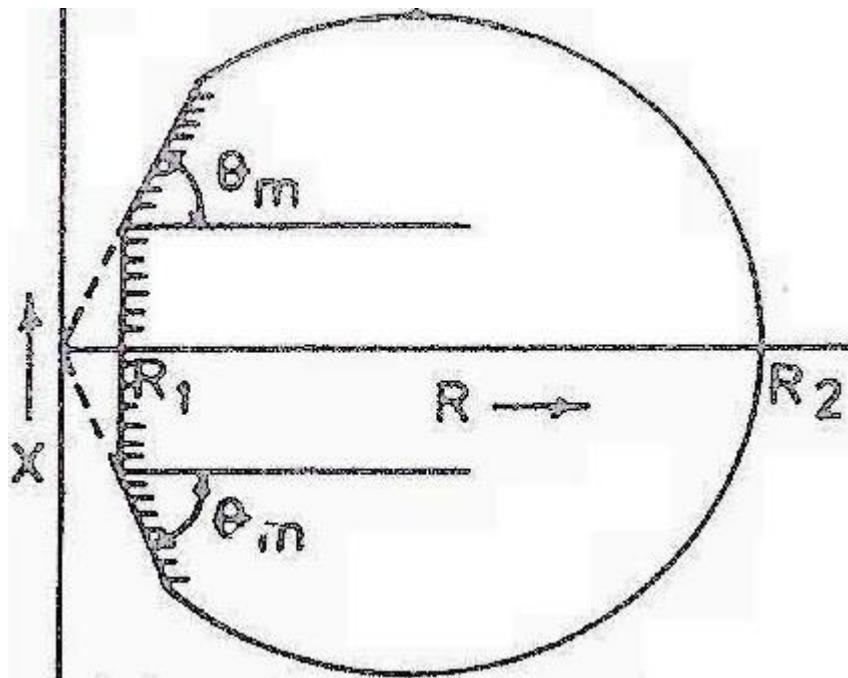
The basic objective in designing the filter is to select the filter admittance Y_{Fh} in order to minimize V_h or satisfy the constraints on V_h . The problem of designing a filter is complicated by the uncertainty about the network admittance (Y_{Sh}). There are two possible representations of system impedance in the complex plane where

(a) impedance angle is limited

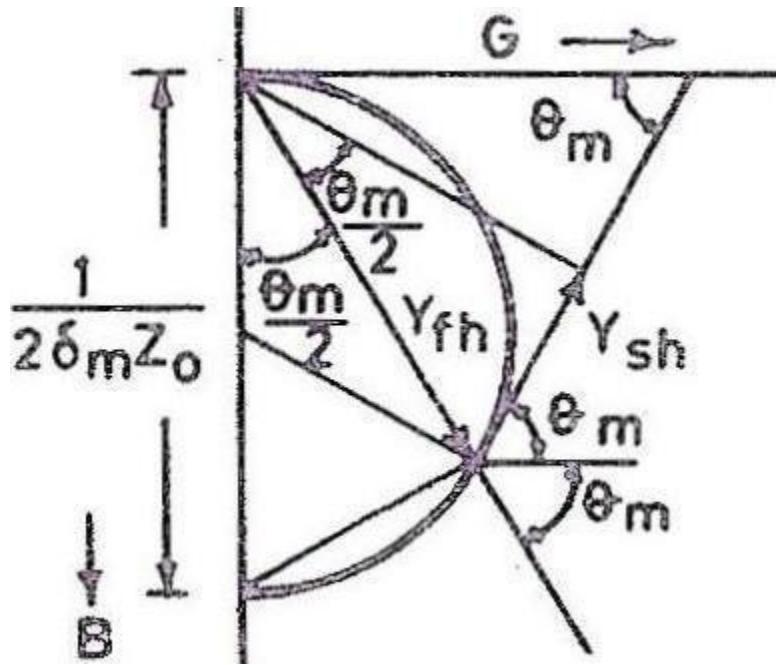


This allows a simplified computation of the optimum value of Q . In computing the optimum value of Q , we need to minimize the maximum value of V_h . The optimum value of Q corresponds to the lowest value of the upper limit on V_h .

(b) the impedance is limited both in angle and impedance



The value of Y_h is reduced if the detuning parameter δ is maximum = δ_m . For a specified value δ_m and X_0 , the locus of the filter impedance as Q is varied is a semicircle in the 4th quadrant of the G-B plane as shown below.



The optimum value of Q can be obtained from game-theoretic analysis. If one selects Y_{Fh} arbitrarily (the tip of Y_{Fh} lying along the semicircle), the network can select Y_{sh} such that the vector Y_h is perpendicular to the vector Y_{sh} and ensure Y_h is minimum. To maximize the minimum magnitude of Y_h , it is necessary to have Y_{sh} tangential to the circle. Thus, we select Y_{Fh} to maximize Y_h when the network tries to minimize it.

Design of High Pass Filter

For harmonic frequencies of order equal to or higher than 17, a common second order high pass filter is provided. By defining the following parameters

$$h_0 \omega_1 = 1/\sqrt{LC}, Z_0 = \sqrt{L/C}, \sigma = R/Z_0$$

The following values can be chosen

$$0.5 < \sigma < 2$$

$$h_0 \leq \sqrt{2} h_{min}$$

where h_{min} is the smallest value of h to be handled by the filter. The choice of h_0 given above implies that the filter impedance at h_{min} has decreased approximately to the value of R .

The filter impedance is given by

$$Z_f = \frac{Z_0 [\sigma + j(h_0/h) \cdot (\sigma^2 - 1 - (\sigma h_0/h)^2)]}{1 + (\sigma h_0/h)^2}$$

The reactive power supplied by the filter is

$$Q_f = (h_0 / (h_0^2 - 1)) \cdot (V_1^2 / Z_0)$$

The filtering is improved if Q_f is increased and higher value of h_0 can be chosen. Hence, it is advantageous in designing high pass filter to exclude six pulse operation.

Protection of Filters

The filter is exposed to overvoltage during switching in and the magnitude of this overvoltage is a function of the short-circuit ratio (higher with low values of SCR) and the saturation characteristics of the converter transformer.

During switching in, the filter current (at filter frequencies) can have magnitudes ranging from 20 to 100 times the harmonic current in normal (steady-state) operation. The lower values for tuned filters and higher values are applicable to high pass filters. These overcurrents are taken into consideration in the mechanical design of reactor coils.

When filters are disconnected, their capacitors remain charged to the voltage at the instant of switching. The residual direct voltages can also occur on bus bars. To avoid, the capacitors may be discharged by short-circuiting devices or through converter transformers or by voltage transformers loaded with resistors.

If the network frequency deviates from the nominal value, higher currents and losses will result in AC filters. If they exceed the limits,

3

ANALYSIS OF HVDC CONVERTER

3.1 INTRODUCTION

In the previous chapter, we looked at the converter circuits – both for Line Commutated, (current source) Converters (LCC) and Voltage Source Converters (VSC). The Graetz Bridge is the basic building block in LCC and also in VSC based HVDC converters (in multi-pulse converters). In twelve pulse LCC (which is a common configuration), two Graetz bridges are connected in series on the DC side and in parallel on the AC side. Typically, a twelve pulse LCC is fed by three single phase transformers, each with three windings (one primary and two secondary). One set of secondary windings, connected in star, feed one bridge while the other set of secondary windings, connected in delta, feed the second bridge. A UHV DC converter is made up of two twelve pulse converters (4 bridges) connected in series on the DC side.

In this chapter, we will analyze both LCC and VSC configurations and study the converter characteristics.

3.2 ANALYSIS OF LINE COMMUTATED CONVERTER

In the previous chapter, we assumed that only one valve in a commutation group of a bridge conducts. In other words, the current transfers instantaneously from one valve to the next valve when the latter is fired.

Due to the leakage inductance of the converter transformer and the impedance in the supply network, the current in a valve cannot change suddenly and thus commutation from one valve to the next cannot be instantaneous. For example, when valve 3 is fired, the current transfer from valve 1 to valve 3 takes a finite period during which both valves are conducting. This is called overlap and its duration is measured by the overlap (commutation) angle ' α '.

Each interval of the period of supply can be divided into two subintervals (see Fig. 3.1). In the first subinterval, three valves are conducting and in the second subinterval, two valves are conducting. This is based on the assumption that the overlap angle is less than 60° . As the overlap angle increases to 60° , there is no instant when only two valves are conducting. As the overlap angle increases beyond 60° , there is a finite period during an interval, when four valves conduct and the rest of the interval during which three valves conduct. Thus there are three modes of the converter as follows:

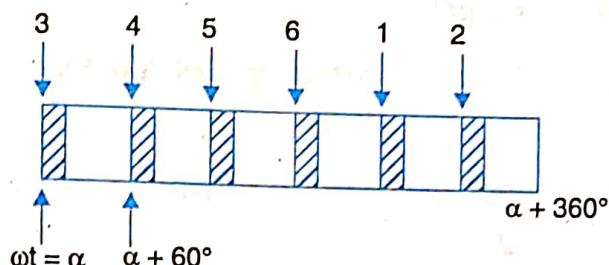


Fig. 3.1: Timing diagram

1. Mode 1—Two and three valve conduction ($u < 60^\circ$)

2. Mode 2—Three valve conduction ($u = 60^\circ$)

3. Mode 3—Three and four valve conduction ($u > 60^\circ$)

Depending upon the delay angle α , the mode 2 may be just a point on the boundary of modes 1 and 3. This is explained later.

With the assumptions stated in Chapter 2 for steady state analysis, it is sufficient to consider only one interval of 60 degree duration —say the interval starting with the firing of (conduction of) valve 3.

(i) Analysis of two and three valve conduction mode

For the interval considered, the bridge circuit can be reduced to that shown in Fig. 3.2.

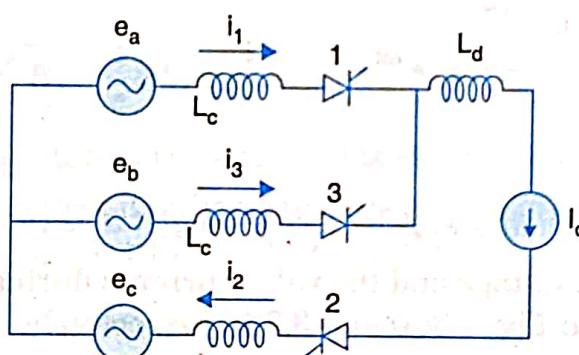


Fig. 3.2: Equivalent circuit for 3 valve conduction

For this circuit,

$$e_b - e_a = L_c \left(\frac{di_3}{dt} - \frac{di_1}{dt} \right) \quad (3.1)$$

The L.H.S. in the above equation is called the commutating emf whose value is given by

$$e_b - e_a = \sqrt{2} E_{LL} \sin \omega t \quad (3.2)$$

which is also the voltage across valve 3 before it starts conducting. Since

$$i_1 = I_d - i_3 \quad (3.3)$$

we get, $\sqrt{2} E_{LL} \sin \omega t = 2 L_c \frac{di_3}{dt} \quad (3.4)$

Solving the above equation, we get

$$i_3(t) = I_s(\cos \alpha - \cos \omega t), \alpha \leq \omega t \leq \alpha + u$$

where

$$I_s = \frac{\sqrt{2}E_{LL}}{2\omega L_c}$$

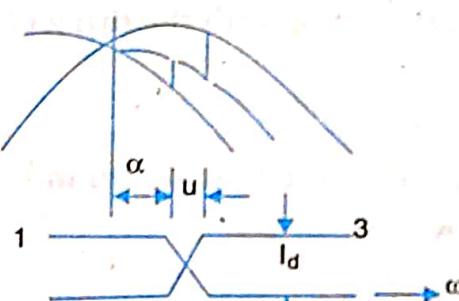
Note that the solution given in 3.5 is obtained from the initial condition

$$i_3(\omega t = \alpha) = 0$$

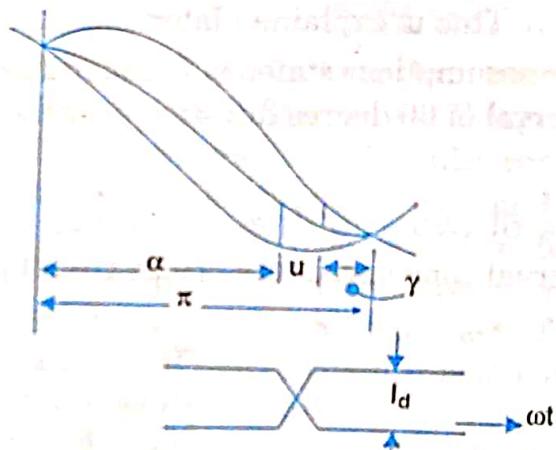
At

$$\omega t = \alpha + u, i_3 = I_d. \text{ This gives}$$

$$I_d = I_s [\cos \alpha - \cos(\alpha + u)]$$



(a)



(b)

Fig. 3.3: Voltage and current waveform during firing of a valve (a) rectifier; (b) inverter

The waveforms of direct voltage and the valve currents during commutation for a rectifier and an inverter are shown in Fig. 3.3(a) and 3.3(b) respectively. It is to be noted that during

commutation, the instantaneous dc voltage is $\frac{-3}{2}e_c \left(\frac{e_a + e_b}{2} - e_c \right)$ instead of $(e_b - e_c)$.

Average direct voltage

The average direct voltage can be obtained as

$$\begin{aligned}
 V_d &= \frac{3}{\pi} \left[\int_{\alpha}^{\alpha+u} \frac{-3}{2} e_c d(\omega t) + \int_{\alpha+u}^{\alpha+60^\circ} (e_b - e_c) d(\omega t) \right] \\
 &= \frac{3}{\pi} \left[\int_{\alpha}^{\alpha+60^\circ} e_{bc} d(\omega t) - \int_{\alpha}^{\alpha+u} \frac{e_b - e_a}{2} d(\omega t) \right] \\
 &= V_{do} \cos \alpha - \frac{3}{2\pi} \int_{\alpha}^{\alpha+u} \sqrt{2}E_{LL} \sin \omega t d(\omega t) \\
 &= V_{do} \cos \alpha - \frac{3}{2\pi} \sqrt{2}E_{LL} [\cos \alpha - \cos(\alpha + u)]
 \end{aligned} \tag{3.9}$$

Since $\frac{3}{\pi} \sqrt{2} E_{LL} = V_{do}$, we get

$$V_d = \frac{V_{do}}{2} [\cos \alpha + \cos(\alpha + u)] \quad (3.10)$$

The equation (3.8) can be substituted in (3.9) to yield,

$$V_d = V_{do} \left(\cos \alpha - \frac{I_d}{2I_s} \right) = V_{do} \cos \alpha - R_c I_d \quad (3.11)$$

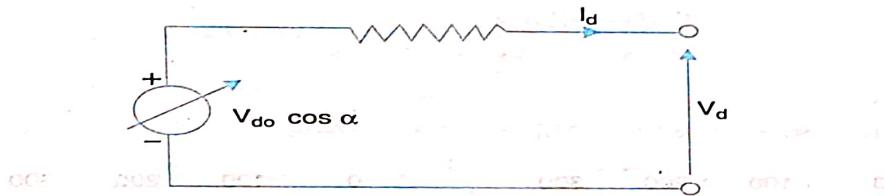


Fig. 3.4: Equivalent circuit of a bridge converter

where,

$$R_c = \frac{3}{\pi} \omega L_c = \frac{3}{\pi} X_c \quad (3.12)$$

R_c is called equivalent commutation resistance. It is something analogous to armature reaction in DC machines in the sense that it only represents a voltage drop and not a power loss. The equivalent circuit of the bridge rectifier is shown in Fig. 3.4.

DC voltage and valve voltage waveforms

Figure 3.5 shows the waveform of the voltage across the converter bridge (V_d). The valve voltage waveform (for a rectifier) is shown in Fig. 3.6. The valve voltage has now 8 jumps. The two major jumps occur at the firing and the turning off of the valve and are given by

$$V_{j1} = \sqrt{2} E_{LL} \sin \alpha$$

$$V_{j2} = \sqrt{2} E_{LL} \sin(\alpha + u)$$

The remaining 6 jumps can be divided into two groups, the first group composed of jumps that are equal in magnitude to $\frac{V_{j1}}{2}$ and the second group of jumps with magnitudes $\frac{V_{j2}}{2}$. These voltage jumps result in extra losses in the damper or snubber circuit of the valve.

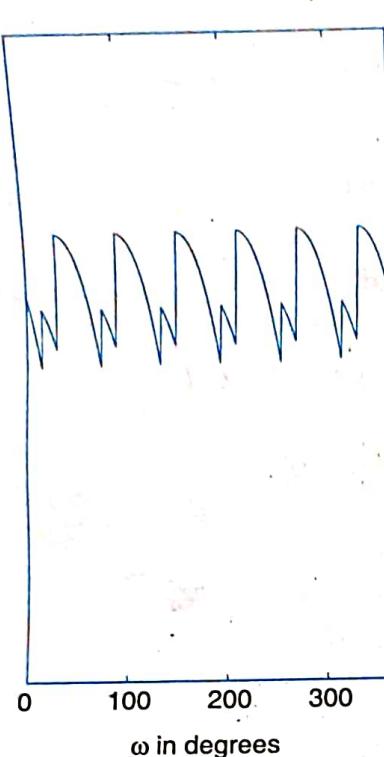


Fig. 3.5: DC voltage waveform

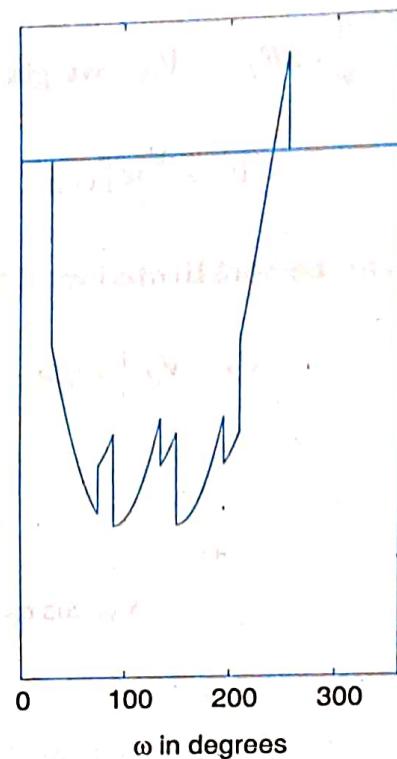


Fig. 3.6: Valve voltage waveform

Inverter equations

For an inverter, it is usual to define an angle of advance β as

$$\beta = \pi - \alpha \quad \text{if triggered at 110 degrees, the current is 0} \quad (3.13)$$

and use opposite polarity for the dc voltage with voltage rise opposite to the direction of current. Thus,

$$\begin{aligned} V_{di} &= \frac{-V_{doi}}{2} [\cos \alpha + \cos(\alpha + u)] \\ &= \frac{-V_{doi}}{2} [\cos(\pi - \beta) + \cos(\pi - \gamma)] \\ &= \frac{V_{doi}}{2} [\cos \beta + \cos \gamma] \end{aligned} \quad (3.14)$$

where the extinction angle γ is defined as

$$\gamma = \beta - u = \pi - \alpha - u \quad (3.15)$$

Similarly, it can be shown that

$$\begin{aligned} V_{di} &= V_{doi} \cos \beta + R_{ci} I_d \\ &= V_{doi} \cos \gamma - R_{ci} I_d \end{aligned} \quad (3.16)$$

The subscript 'i' refers to the inverter.

Comparing equations (3.14) and (3.16) with (3.10) and (3.11) shows that the inverter equations are obtained by substituting γ for α in the rectifier equations. However it is to be noted that while α is directly controllable, γ is not.

AC current and DC voltage harmonics

The waveforms of the valve currents and the current in the valve winding are distorted. Thus, the expression for the fundamental component of the AC current derived for the case with no overlap is not valid. The actual expression for the current can be derived from Fourier analysis and is given by

$$I_1 = [I_{11}^2 + I_{12}^2]^{1/2} \quad (3.17)$$

$$I_{11} = I_1 \cos \phi = \frac{\sqrt{6}}{\pi} I_d \left[\frac{\cos \alpha + \cos(\alpha + u)}{2} \right] \quad (3.18)$$

$$I_{12} = I_1 \sin \phi = \frac{\sqrt{6}}{\pi} I_d \left[\frac{2u + \sin 2\alpha - \sin 2\delta}{4(\cos \alpha - \cos \delta)} \right] \quad (3.19)$$

where ϕ is the power factor angle and $\delta = \alpha + u$

From the above expressions, the power factor angle can be obtained as

$$\tan \phi = \frac{2u + \sin 2\alpha - \sin 2\delta}{\cos 2\alpha - \cos 2\delta} \quad (3.20)$$

The harmonic components in the AC current are also altered. These are reduced from the values calculated with no overlap. The reduction factor is given by

$$\frac{I_h}{I_{ho}} = \frac{1}{2x} [H^2 + K^2 - 2HK \cos(2\alpha + u)]^{1/2} \quad (3.21)$$

where

$$H = \frac{\sin \left[(h+1) \frac{u}{2} \right]}{h+1}, K = \frac{\sin \left[(h-1) \frac{u}{2} \right]}{h-1} \quad (3.22)$$

$$x = \frac{1}{2} [\cos \alpha - \cos(\alpha + u)] \quad (3.23)$$

$I_{ho} = \frac{\sqrt{6}}{\pi} \frac{I_d}{h}$ = harmonic component with no overlap. Figure 3.7 shows this reduction factor for the case $\alpha = 30^\circ$. It can be seen that all the harmonics especially of higher order, decrease sharply with increasing values of u and the reduction factor lies in the range 0.1 to 0.2.

The harmonics in the direct voltage are also altered due to overlap. It can be shown that

$$\frac{V_h}{V_{do}} = \frac{1}{\sqrt{2}} [F^2 + G^2 - 2FG \cos(2\alpha + u)]^{1/2} \quad (3.24)$$

$$F = \frac{\cos \left[(h+1) \frac{u}{2} \right]}{h+1}, G = \frac{\cos \left[(h-1) \frac{u}{2} \right]}{h-1} \quad (3.25)$$

where

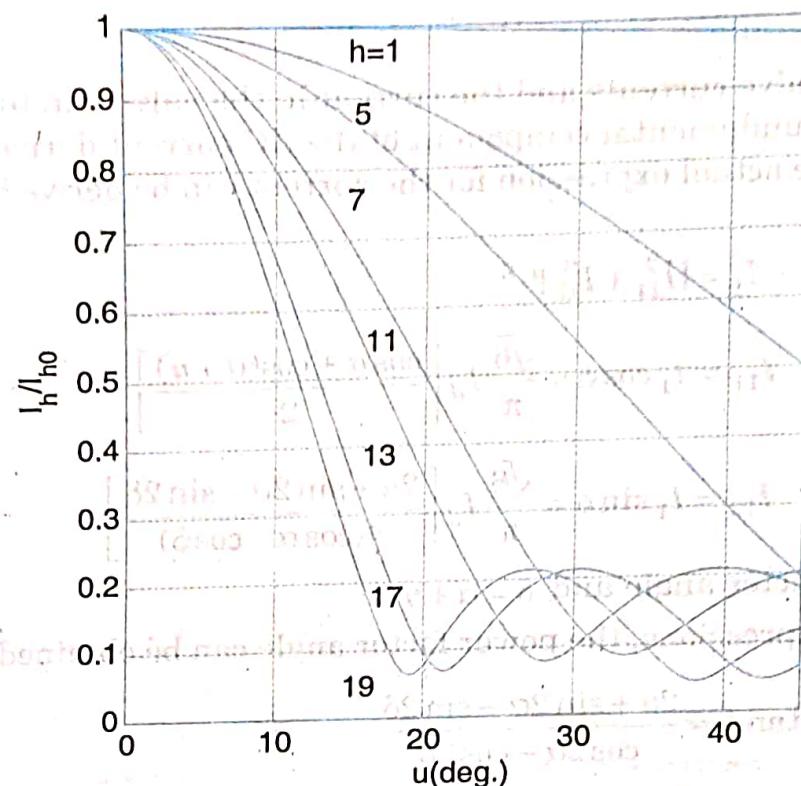


Fig. 3.7: Variation of AC current harmonics with overlap

Figure 3.8 shows $\left(\frac{V_{12}}{V_{do}}\right)$ for different values of u and α .

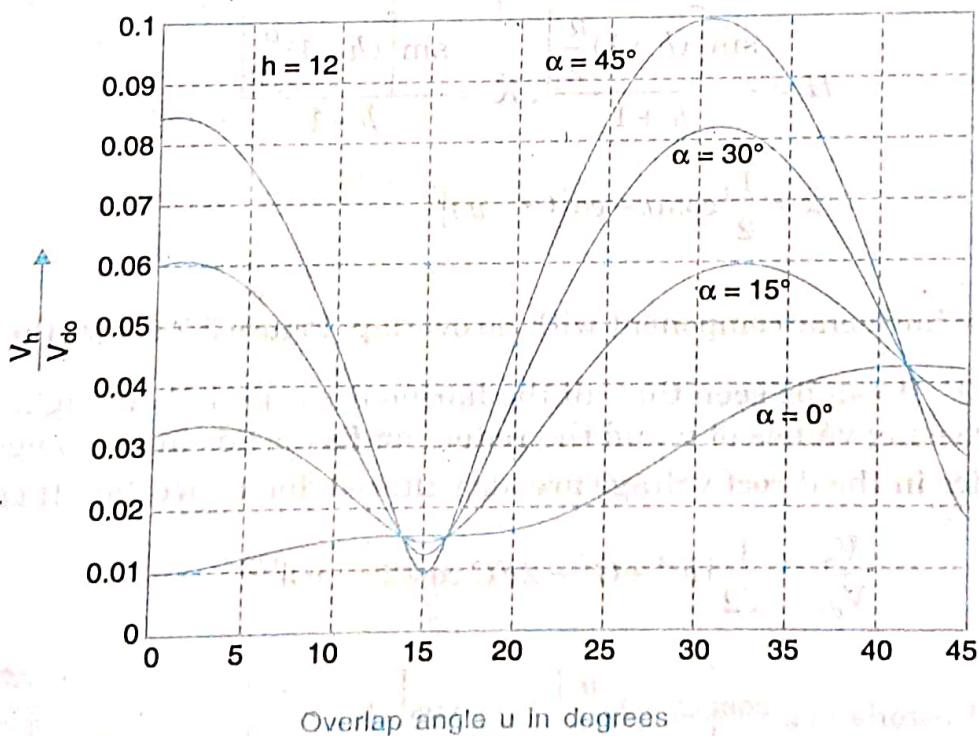


Fig. 3.8: Variation of DC voltage harmonics with overlap

Example 1

If the DC current varies with time, prove that $\frac{I_{d1} + I_{d2}}{2} = I_s [\cos \alpha - \cos(\alpha + u)]$ where I_{d1} is the DC current at the beginning of the commutation ($\omega t = \alpha$) and I_{d2} is the DC current at the end of the commutation ($\omega t = \alpha + u$). Assume two and three valve conduction mode.

Solution

Consider the circuit shown in Fig. 3.2. Substituting Eq. (3.3) in (3.1), we get

$$e_b - e_a = 2L_c \frac{di_3}{dt} - L_c \frac{dI_d}{dt}$$

Note: The above equation replaces (3.4))

Substituting Eq. (3.2) in the above equation, we get

$$2L_c i_3(t) = \frac{1}{\omega} \int_{\alpha}^{\omega t} (e_b - e_a) d(\omega t) + \frac{L_c}{\omega} \int_{\alpha}^{\omega t} \frac{dI_d}{dt} d(\omega t)$$

$$i_3(t) = \frac{\sqrt{2}E_{LL}}{2X_c} [\cos \alpha - \cos \omega t] + \frac{1}{2} [I_d(\omega t) - I_{d1}]$$

Since, $i_3(\omega t = \alpha + u) = I_{d2}$, we get

$$I_{d2} = I_s [\cos \alpha - \cos(\alpha + u)] + \frac{1}{2} [I_{d2} - I_{d1}]$$

From the above, we get the desired result

$$\frac{I_{d1} + I_{d2}}{2} = I_s [\cos \alpha - \cos(\alpha + u)]$$

Example 2

Prove that $\frac{V_d}{V_{don}} = \bar{E} \cos \alpha - \frac{\bar{X}_c}{2} \frac{I_d}{I_{dn}}$ where, the subscript n indicates rated values and \bar{X}_c is the leakage reactance of the converter transformer expressed on its own base. \bar{E} is the AC voltage expressed in per unit of the rated voltage.

Solution

From Eqs. (3.11) and (3.12), we get

$$\frac{V_d}{V_{don}} = \frac{V_{do}}{V_{don}} \cos \alpha - \frac{3}{\pi} \frac{X_c I_{dn}}{V_{don}} \left(\frac{I_d}{I_{dn}} \right)$$

Since, $V_{don} = \frac{3\sqrt{2}}{\pi} E_{an}$ where E_{an} is the rated line to AC voltage (on the valve side), we get

$$\frac{V_d}{V_{don}} = \frac{E_a}{E_{an}} \cos \alpha - \frac{X_c I_{dn}}{\sqrt{2} E_{an}} \left(\frac{I_d}{I_{dn}} \right)$$

where E_a is the actual line to AC voltage (Note that $V_{do} = \frac{3\sqrt{2}}{\pi} E_a$).

Noting that the rated AC current (including the harmonic current components), denoted by I_{an} , given by

$$I_{an} = \sqrt{\frac{2}{3}} I_{dn}$$

Since

$$Z_b = \frac{E_{an}}{\sqrt{3} I_{an}} = \frac{E_{an}}{\sqrt{2} I_{dn}}$$

where, Z_b is the base impedance (on the transformer base), we get finally,

$$\frac{V_d}{V_{don}} = \bar{E} \cos \alpha - \frac{\bar{X}_c}{2} \left(\frac{I_d}{I_{dn}} \right)$$

Example 3

Prove that $\frac{I_d}{I_{dn}} = \frac{\bar{E}}{\bar{X}_c} [\cos \alpha - \cos(\alpha + u)]$

Solution

This follows from Eq. (3.5) and expressing the DC current and the AC voltage in per unit of their rated values (as done in Example 2). Noting that $\frac{\sqrt{2} X_c I_{dn}}{E_{an}} = \frac{X_c}{Z_b} = \bar{X}_c$, we can derive the above expression.

(ii) Three and four valve conduction mode

Although two and three valve conduction mode is the normal mode of operation, during DC line faults or a dip in the AC voltage, it is likely that the overlap angle u would be larger and may exceed 60° .

When the overlap angle exceeds 60° , the minimum number of valves conducting are three and there are intervals when four valves are conducting. This is because when a commutation process is started, the previous commutation process is not yet completed. For example, when valve 3 is fired, the valves 1, 6, and 2 are still conducting. The equivalent circuit for this condition is shown in Fig. 3.9. It can be observed that $v_d = 0$.

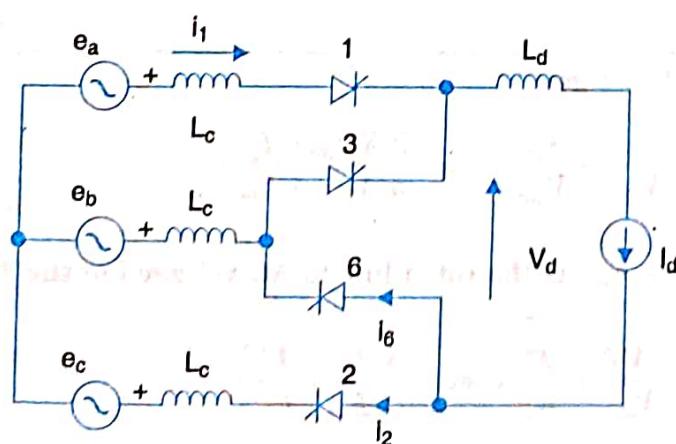


Fig. 3.9: Equivalent circuit for four valve conduction

(a) For $\alpha \leq \omega t \leq \alpha + u - 60^\circ$

$$L_c \frac{di_1}{dt} = e_a = \sqrt{\frac{2}{3}} E_{LL} \sin(\omega t + 150^\circ)$$

$$L_c \frac{di_2}{dt} = -e_c = \sqrt{\frac{2}{3}} E_{LL} \cos \omega t$$

Solving for i_1 and i_6

$$i_1 = I_s^1 \sin(\omega t + 60^\circ) + A \quad (3.26)$$

$$i_6 = I_d - i_2 = I_d - I_s^1 \sin \omega t + C \quad (3.27)$$

where

$$I_s^1 = \sqrt{\frac{2}{3}} \frac{E_{LL}}{\omega L_c} = \frac{2}{\sqrt{3}} I_s$$

The constant A can be determined from initial condition

$$i_1(\omega t = \alpha) = I_d = I_s^1 \sin(\alpha + 60^\circ) + A \quad (3.28)$$

The constant C can be determined from the final condition

$$i_6(\omega t = \alpha + u - 60^\circ) = 0 = I_d - I_s^1 \sin(\alpha + u + 60^\circ) + C = 0 \quad (3.29)$$

(b) For, $\alpha + u - 60^\circ \leq \omega t \leq \alpha + 60^\circ$

Here, with 3 valves conducting

$$2L_c \frac{di_1}{dt} = -\sqrt{2} E_{LL} \sin \omega t$$

Solving for i_1 we get

$$i_1 = I_s \cos \omega t + B \quad (3.30)$$

I_s is defined by equation (3.6)

The constant B can be determined from the continuity equation

$$\begin{aligned} i_1(\omega t = \alpha + u - 60^\circ) &= I_s^1 \sin(\alpha + u) + A \\ &= I_s \cos(\alpha + u - 60^\circ) + B \end{aligned} \quad (3.31)$$

From symmetry, we have

$$i_1(\omega t = \alpha + 60^\circ) = i_6(\omega t = \alpha)$$

$$I_s \cos(\alpha + 60^\circ) + B = I_d - I_s^1 \sin(\alpha + u) + C \quad (3.32)$$

After some manipulations we can obtain

$$I_d = \frac{I_s^1}{2} [\cos(\alpha - 30^\circ) - \cos(\alpha + u + 30^\circ)] \quad (3.33)$$

Average Direct Voltage

The expression for the average direct voltage is obtained as

$$V_d = \frac{3}{\pi} \frac{\alpha + 60^\circ}{\alpha + u - 60^\circ} = \frac{3}{2} e_c d(\omega t)$$

$$e_c = -E_m \cos \omega t, E_m = \sqrt{\frac{2}{3}} E_{LL}$$

(Note, that $v_d = 0$ when $\alpha \leq \omega t \leq \alpha + u - 60^\circ$)

$$V_d = \frac{3}{\pi} \frac{3}{2} E_m [\sin(\alpha + 60^\circ) - \sin(\alpha + u - 60^\circ)]$$

$$V_d = \frac{\sqrt{3}}{2} V_{do} [\cos(\alpha - 30^\circ) + \cos(\alpha + u + 30^\circ)]$$

From (3.33) and (3.34), we get

$$\begin{aligned} V_d &= V_{do} \left[\sqrt{3} \cos(\alpha - 30^\circ) - \frac{3}{2} \frac{I_d}{I_s} \right] \\ &= \sqrt{3} V_{do} \cos(\alpha - 30^\circ) - 3 R_c I_d \end{aligned} \quad (3.35)$$

Comparing equation (3.35) with (3.11) shows that the equivalent commutating resistance for this case is three times that for the case with overlap angle less than 60° . When the delay angle is zero, the overlap angle u reaches a value of 60° when the current I_d increases to

$$I_d = I_s [1 - \cos 60^\circ] = \frac{1}{2} I_s$$

At $u = 60^\circ$, three valves are conducting all the time. If the current is increased further, u would tend to increase further, however, this is not possible unless $\alpha \geq 30^\circ$. For values of $\alpha < 30^\circ$, an increase in direct current is possible only when α is increased and the overlap angle is maintained at 60° . The reason why the overlap cannot be increased beyond 60° for $\alpha < 30^\circ$ is evident from Fig. 3.10. When valves 2 and 6 are still conducting, the anode of valve 3 is at a potential of

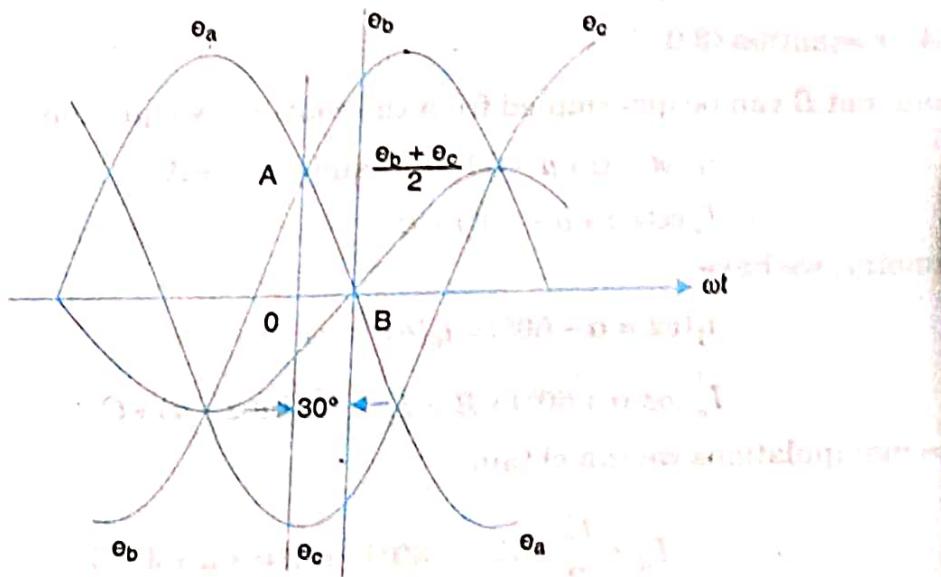


Fig. 3.10: Figure explaining minimum delay angle = 30° if overlap angle = 60° or greater

$\left(\frac{e_b + e_c}{2}\right) = \left(\frac{-e_a}{2}\right)$ and the cathode is at a potential of e_a . Hence unless e_a is negative, the valve 3 cannot conduct (even after raising the gate pulse) and this is possible only for $\alpha \geq 30^\circ$. Thus, there is an intermediate mode when the value of overlap angle remains constant at 60° . In this mode, the increase in direct current is accompanied by automatic increase in the firing angle.

DC and valve voltage wave forms

The instantaneous voltage across the converter bridge (v_d) and the valve voltage for the 3 and 4 valve conduction modes are shown in Fig. 3.11 and 3.12 respectively (for $\alpha = 45^\circ$ and $u = 75^\circ$). The instantaneous voltage across the bridge can have both positive and negative excursions followed by periods of zero magnitude. The valve voltage has 6 jumps with three of them having the magnitude

$$V_{j1} = \sqrt{\frac{3}{2}} E_{LL} \sin(\alpha - 30^\circ)$$

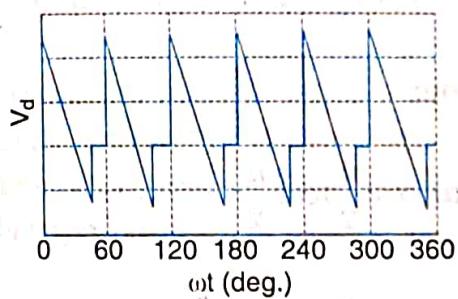


Fig. 3.11: DC voltage waveform for $\alpha = 45^\circ$ $u = 75^\circ$

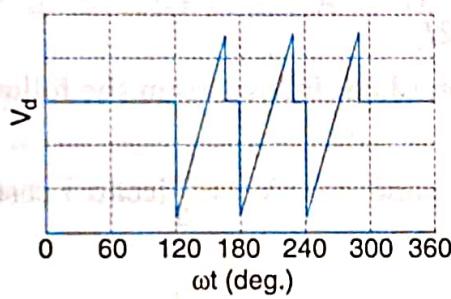


Fig. 3.12: Valve voltage waveform for $\alpha = 45^\circ$, $u = 75^\circ$

The other three jumps have the magnitudes given by.

$$V_{j2} = \sqrt{\frac{3}{2}} E_{LL} \sin(\alpha + u + 30^\circ)$$

3.3 LCC BRIDGE CHARACTERISTICS

[A] Rectifier

The rectifier in general has three modes.

- (1) First mode: Two and three valve conduction mode ($u < 60^\circ$)
- (2) Second mode: Three valve conduction mode $0 \leq \alpha \leq 30^\circ$; ($u = 60^\circ$)
- (3) Third mode: Three and four valve conduction mode $\alpha > 30^\circ$; ($60^\circ < u \leq 120^\circ$)

As the DC current continues to increase, the converter operation changes over from mode 1 to 2 and finally to mode 3.

The DC voltage continues to decrease until it reaches zero.

For, $\alpha \geq 30^\circ$ mode 2 is bypassed.

for modes (1) and (3) we have respectively

$$\frac{\bar{V}_d}{V_{do}} = \frac{V_d}{V_{do}} = \cos \alpha - \frac{I_d}{2I_s} \quad (3.35)$$

$$\frac{V_d}{V_{do}} = \sqrt{3} \cos(\alpha - 30^\circ) - \frac{3I_d}{2I_s} \quad (3.36)$$

The voltage and current characteristics are linear (with different slopes) in these cases.

For mode (2), $u = 60^\circ$. For $u = \text{constant}$, the characteristics are elliptical and the equation is given by

$$\left(\frac{\bar{V}_d}{\cos \frac{u}{2}} \right)^2 + \left(\frac{\bar{I}_d}{\sin \frac{u}{2}} \right)^2 = 1 \quad (3.38)$$

$$\text{where } \bar{I}_d = \frac{I_d}{2I_s}$$

Equation (3.38) follows from the following relations

$$\bar{V}_d = \frac{1}{2} [\cos \alpha + \cos(\alpha + u)] = \cos(\alpha + \frac{u}{2}) \cos \frac{u}{2} \quad (3.39)$$

$$\bar{I}_d = \frac{1}{2} [\cos \alpha - \cos(\alpha + u)] = \sin(\alpha + \frac{u}{2}) \sin \frac{u}{2} \quad (3.40)$$

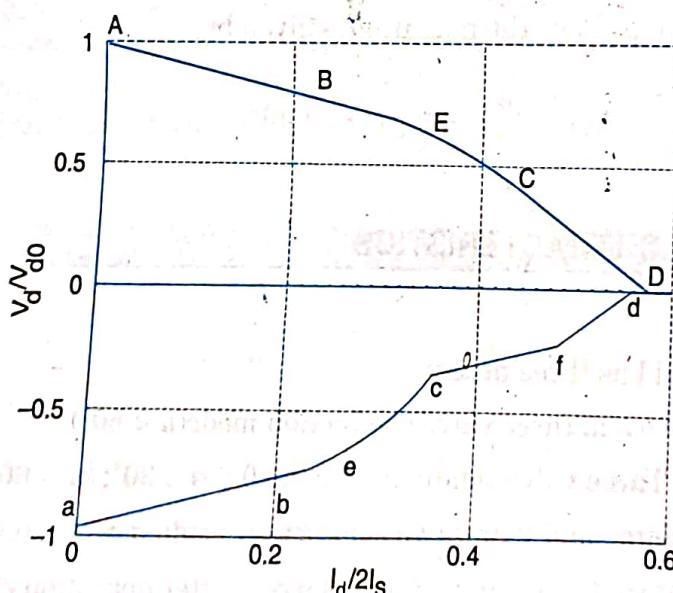


Fig. 3.13: Converter V_d – I_d characteristics

The boundary for the rectifier operation is shown in the Fig. 3.13. The coordinates of points A, B, C, D and E on the boundary are given in Table 3.1. The point E corresponds to the maximum power output of the converter.

Table 3.1: Boundary of Rectifier Characteristics

Point	α	u	\bar{I}_d	\bar{V}_d
A	0	0	0	1.0
B	0	60°	0.25	0.75
C	30°	60°	$\sqrt{3}/4$	$\sqrt{3}/4$
D	30°	120°	$1/\sqrt{3}$	0
E	15°	60°	$1/(2\sqrt{2})$	$\sqrt{3}/(2\sqrt{2})$

3. [B] Inverter

The inverter characteristics are similar to the rectifier characteristics. However, the operation as an inverter requires a minimum commutation margin angle during which the voltage across the valve is negative. Hence the operating region of an inverter is different from that for a rectifier.

The commutation margin angle (ξ) is equal to the extinction angle (γ) only for values of $\beta \leq 60^\circ$. This is clear from Fig. 3.14(a). The voltage across the valve has a positive dent D because of the succeeding commutation. This dent normally occurs (for $\beta \leq 60^\circ$) after the sinusoidal voltage (on which it is superposed) has become positive.

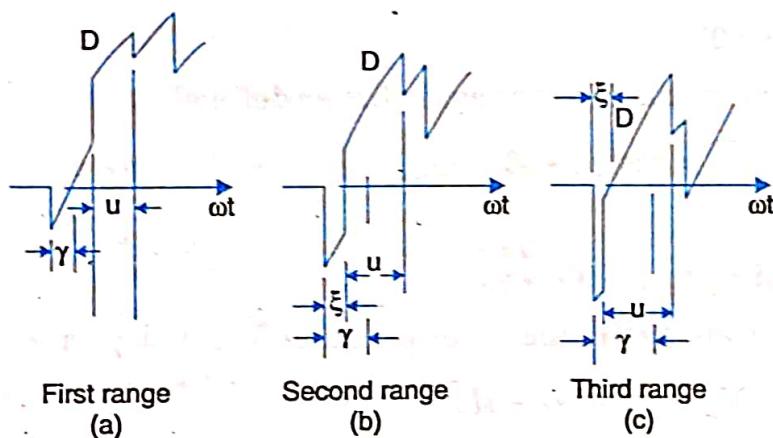


Fig. 3.14: Relationship between inverter angles

Hence under this condition $\xi = \gamma$. With increased overlap and consequently earlier ignition (firing) of the valve, the dent encroaches on the period in which the valve voltage would otherwise be negative [see Fig. 3.14(b)] and this makes $\xi < \gamma$. After the front of the dent becomes entirely negative, further advance of the dent (Fig. 3.14(c)] does not decrease commutation margin further. Thus, the margin angle (ξ) has different relationship to γ depending on the range of operation, which is summarized below.

First range: $\beta \leq 60^\circ$

$$\xi = \gamma$$

Second range: $60^\circ < \beta < 90^\circ$

$$\xi = 60^\circ - u = \gamma - (\beta - 60^\circ)$$

Third range: $\beta > 90^\circ$

$$\xi = \gamma - 30^\circ$$

In the inverter operation, it is necessary to maintain a certain minimum margin angle ξ_0 . This results in 3 sub-modes of the first mode. The overall inverter characteristics are described below.

Mode 1

1(a) $\beta < 60^\circ$ for values of $u < (60^\circ - \xi_0)$.

The characteristics are linear defined by

$$\bar{V}_d = \cos \gamma_0 - \bar{I}_d$$

1(b) $60^\circ < \beta < 90^\circ$ for values of $u < 60^\circ - \xi_0$.
 $u = 60^\circ - \xi_0 = 60^\circ - \gamma_0 = \text{constant}$

As discussed earlier, the characteristics are elliptical defined by equation (3.38)

1(c) $90^\circ < \beta < 90^\circ + \xi_0$ for the values of u in the range

$$60^\circ - \xi_0 \leq u \leq 60^\circ$$

The characteristics in this case are again linear defined by

$$\bar{V}_d = \cos(\gamma_0 + 30^\circ) - \bar{I}_d$$

Mode 2

For $u > 60^\circ$ corresponding to $\beta > 90^\circ + \gamma_0$

The characteristics are again linear but with a different slope and defined by

$$\bar{V}_d = \sqrt{3} \cos \gamma_0 - 3\bar{I}_d$$

The boundary of the inverter operation for a value of $\xi_0 = 15^\circ$ is shown in Fig. 3.13.

The coordinates of points a, b, c, d and f on the boundary are given in Table 3.2.

Table 3.2: Boundary of Inverter Characteristics

Point	γ	u	\bar{I}_d	\bar{V}_d
a	15°	0	0	-0.966
b	15°	45°	0.233	-0.733
c	45°	45°	0.354	-0.354
f	45°	60°	0.483	-0.224
d	45°	90°	0.558	0
e	22.5°	45°	0.271	-0.654

The maximum power supplied by the inverter occurs at $\gamma = 22.5^\circ$ and $u = 45^\circ$ (point e).

In the normal operation of the converter \bar{I}_d is in the range of 0.08 to 0.1. Hence, only the first linear portion of the characteristics (both for rectifier and inverter) is of importance in the converter control.

Example 4

A Graetz bridge operates with a delay angle of 15° . The leakage reactance of the transformer is 10 ohms. The line to line AC voltage is 85 kV. Compute the overlap angle and DC voltage for (i) $I_d = 2000$ A, (ii) $I_d = 4500$ A.

Solution

A rectifier can operate with (i) $u < 60^\circ$, (ii) $u = 60^\circ$, or (iii) $u > 60^\circ$. To determine the operating mode, we need to know the boundaries of the first two modes. The boundary (upper limit for I_d) for mode 1

is given by $\bar{I}_{d1} = \frac{1}{2} [\cos \alpha - \cos(\alpha + 60^\circ)]$

$$\bar{I}_{d1} = I_s [\cos 15^\circ - \cos 75^\circ]$$

$$I_s = \frac{\sqrt{2} \times 85}{2 \times 10} = 6 \text{ kA}$$

$$I_{d1} = 4.25 \text{ kA}$$

Similarly the upper limit on I_d , when $u = 60^\circ$ is given by

$$I_{d2} = I_s [\cos 30^\circ - \cos 90^\circ] = 5.2 \text{ kA}$$

(i) When $I_d = 2000$ A, we have mode 1 with $u < 60^\circ$

$$\bar{V}_d = \cos \alpha - \bar{I}_d = \cos 15^\circ - \frac{2000}{12000} = 0.8$$

$$V_{do} = \frac{3\sqrt{2}}{\pi} E_{LL} = \frac{3\sqrt{2} \times 85}{\pi} = 114.8 \text{ kV}$$

$$V_d = 0.8 V_{do} = 91.8 \text{ kV}$$

The overlap angle u is obtained from

$$\frac{2}{12} = \frac{1}{2} [\cos 15^\circ - \cos(15 + u)]$$

The solution for $u = 35.8^\circ$

(ii) When $I_d = 4500$ A, the mode is $u = 60^\circ$

$\bar{I}_d = \frac{4.5}{12} = 0.375$. \bar{V}_d can be found from

$$\left(\frac{\bar{V}_d}{\cos \frac{u}{2}} \right)^2 + \left(\frac{\bar{I}_d}{\sin \frac{u}{2}} \right)^2 = 1$$

$$\bar{V}_d = \left[1 - \left(\frac{0.375}{\sin 30^\circ} \right)^2 \right]^{\frac{1}{2}} \cos 30^\circ = 0.573$$

$$V_d = 0.573 \times V_{do} = 0.573 \times 114.8 = 65.8 \text{ kV}$$

The firing angle α is obtained from

$$\bar{V}_d = \cos \alpha - \bar{I}_d$$

$$\cos \alpha = \bar{V}_d + \bar{I}_d = 0.573 + 0.375 = 0.948$$

$$\alpha = 18.6^\circ$$

Example 5

A six pulse inverter is operating at a constant margin angle of 18° . The valve side voltage is 70.7 kV (line to line) and the leakage reactance of the converter transformer is 10 ohms . Compute the extinction angle, overlap angle and DC voltage when (i) $I_d = 2500 \text{ A}$ and (ii) $I_d = 4200 \text{ A}$.

Solution

An inverter can operate in either Mode 1 ($u < 60^\circ$, two and three valve conduction mode) or Mode 2 ($u > 60^\circ$, three and four valve conduction mode). Mode 1 can have three sub-modes.

- (a) $\beta < 60^\circ$
- (b) $60^\circ \leq \beta < 90^\circ$
- (c) $90^\circ < \beta \leq 90^\circ + \xi_0$

To identify the operating mode, it is necessary to know the boundaries of the various modes or sub-modes.

Mode 1 (a): $0 \leq I_d < I_{d1}$

$$I_{d1} = I_s (\cos \gamma - \cos \beta), I_s = \frac{\sqrt{2} E_{LL}}{2X_c} = \frac{\sqrt{2} \times 70.7}{2 \times 10} = 5 \text{ kA}$$

$$\gamma = \xi = 18^\circ, \beta = 60^\circ, \text{ Hence } I_{d1} = 2.255 \text{ kA}$$

Mode 1 (b): $I_{d1} \leq I_d \leq I_{d2}$

When $I_d = I_{d2}$, $\beta = 90^\circ$, $\gamma = \xi + 30^\circ$

$$\text{Hence, } I_{d2} = I_s (\cos \gamma - \cos \beta) = 3.346 \text{ kA}$$

Mode 1 (c): $I_{d2} \leq I_d \leq I_{d3}$

When $I_d = I_{d3}$, $\beta = 90^\circ + \xi = 108^\circ$, $\gamma = \xi + 30^\circ$

$$I_{d3} = 5 \times (\cos 48^\circ - \cos 108^\circ) = 4.891 \text{ kA}$$

(i) when $I_d = 2500 \text{ A}$, the inverter is operating in Mode 1 (b). Here, $u = 60 - \zeta = 42^\circ = \text{constant}$

$$\left(\frac{\bar{I}_d}{\sin \frac{u}{2}} \right)^2 + \left(\frac{\bar{V}_d}{\cos \frac{u}{2}} \right)^2 = 1, \bar{I}_d = \frac{2.5}{10} = 0.25$$

$$\bar{V}_d^2 = \left[1 - \left(\frac{0.25}{\sin 21^\circ} \right)^2 \right] \cos^2 21^\circ$$

$$\bar{V}_d = 0.6689, V_d = V_{do} \bar{V}_d = 0.6689 \times \frac{3}{\pi} \times 100 = 63.88 \text{ kV}$$

Since

$$\bar{V}_d = \cos \gamma - \bar{I}_d, \cos \gamma = \bar{V}_d + \bar{I}_d = 0.6689 + 0.25$$

$$\gamma = \cos^{-1}(0.9189) = 23.2^\circ$$

(ii) $I_d = 4200 \text{ A}$. The inverter is operating in Mode I (c). $\bar{I}_d = 0.42$, $\gamma = 48^\circ$

$$\bar{V}_d = \cos \gamma - \bar{I}_d = \cos 48^\circ - 0.42 = 0.2491$$

$$V_d = \bar{V}_d \times V_{do} = 23.79 \text{ kV}$$

To compute overlap angle

$$\bar{I}_d = \frac{1}{2} [\cos \gamma - \cos(\gamma + u)]$$

$$\cos(48^\circ + u) = \cos 48^\circ - 2\bar{I}_d$$

$$= \cos 48^\circ - 0.84$$

$$u = \beta - \gamma = 99.8^\circ - 48^\circ = 51.8^\circ$$

3.4 CHARACTERISTICS OF A TWELVE PULSE CONVERTER

As long as the AC voltages at the converter bus remain sinusoidal (with effective filtering), the operation of one bridge is unaffected by the operation of the other bridge connected in series. In this case, the converter characteristics are as shown in Fig. 3.13 with the assumption that the AC voltages at the converter bus remain constant. The region of rectifier operation can be divided into five modes as follows:

Mode 1 : 4 and 5 valve conduction

$$0 < u < 30^\circ$$

Mode 2 : 5 and 6 valve conduction

$$30^\circ < u < 60^\circ$$

Mode 3 : 6 valve conduction

$$0 < \alpha < 30^\circ; u = 60^\circ$$

Mode 4 : 6 and 7 valve conduction

$$60^\circ < u < 90^\circ$$

Mode 5 : 7 and 8 valve conduction

$$90^\circ < u < 120^\circ$$

It is to be noted that the second mode is a continuation of the first and similarly fifth is a continuation of the fourth. Five valve and seven valve conduction modes are just points on the boundaries corresponding to their previous and following modes. The region corresponding to mode 3 shrinks to a point when α exceeds 30° .

The characteristics of the inverter are similar except that a sub-mode can exist for mode 1 or 2 depending on the value of margin angle chosen (usually for mode 2). The characteristics of this sub-mode are elliptical as explained in the previous section.

When no AC filters are provided and the source reactance is not zero the operation of either bridge is affected by the commutation process taking place in the other bridge. In this case, the operation of the twelve pulse converter is quite complex and there could be additional modes (i) 5 valve conduction and (ii) 6-7-8-7 valve conduction [1]. Also, there could be new mode of 5-6-7-6 valve conduction (instead of 6 valve conduction), depending on the value of coupling factor K , defined by

$$K = \frac{X_S}{X_S + X_T}$$

where X_S is the source reactance and X_T is the converter transformer leakage reactance.

It is to be noted that the interaction between adjacent bridges can be neglected if the converter bus voltages are sinusoidal (when AC filters are provided). However, the presence of the source reactance results in the variation of the magnitude of the bus voltage (unless voltage control is provided at the converter station). This can affect the shape of the converter characteristics.

The analysis of a converter with source impedance, filters and finite smoothing reactor is described in the next section.

3.5 DETAILED ANALYSIS OF CONVERTERS

Here, the assumptions of constant DC current and constant, sinusoidal voltages at the AC bus are relaxed. The analysis takes into account impedances in both the AC and DC networks.

The steady-state solution of HVDC converter equation is periodic. With linear network elements, the equations are also piecewise linear. A method for obtaining fast steady-state solution of the system equations for the general case is described next.

Outline of the method

The method is based on the following assumptions:

1. The system is described by sets of linear differential equations and each set is applicable for particular conduction pattern of the valves in bridge.
2. AC system is symmetrical and source voltages are balanced.
3. Firing pulses are generated at equal intervals of time.

Given the initial conditions and forcing functions, the solution can be obtained analytically over each interval or sub-interval. The solution is periodic in steady-state, each period can be divided into p intervals, where p is the pulse number of the converter. Each interval, in general, can be divided into two sub-intervals as follows:

1. $0 < t < t_1$, corresponding to the conduction of $(m + 1)$ valves.

2. $t_1 < t < T_1$ corresponding to the conduction of m valves. ($T_1 = \frac{T}{p}$, T is the period of the AC voltage).

For example, in a 6-pulse converter, the normal mode consists of 3 and 2 valve conduction with $m = 2$. The derivation of the steady-state solution proceeds from first computing t_1 from a non-linear equation of the form

$$f(t_1) = 0$$